Introduction

One of the most important aspects of a realistic physics system is the ability to detect and resolve the collisions that occur between the objects in the simulation - a snooker game isn’t very fun if we can’t knock balls around by hitting the cue ball with our cue!

The following two tutorials are going to show you the basics behind the process of collision resolution, which will greatly increase the realism of your physics simulation. In this tutorial, we’re going to see how to use collision detection algorithms determine whether two objects are colliding in some way - that is, their shapes are touching or overlapping due to their movement over time. Detecting this, and determining how much overlap, and the positions in space the objects hit each other are the first steps towards creating realistic collision resolution. The next tutorial will deal with collision response. As objects intersecting each other isn’t physically possible, we have to maintain the realism of the simulation by resolving those collisions by separating them out so that they aren’t overlapping, and determining whether any kinetic energy should be transferred from one object to another - such as when we hit that cue ball, sending it flying off down the table.

Collision Volumes

We saw in the previous tutorial in raycasting, that there’s a set of standard collision volumes used to represent most of the physics-enabled objects in our game simulations. Just as with rays, the process of detecting collisions between each combination of these shapes is a little bit different, so we will have to define a series of functions to handle each potential collision that can occur each simulation frame. To this end, in this tutorial we will investigate the most common collisions that we need to detect: sphere versus sphere, AABB versus AABB, and AABB versus sphere.

Collision Detection

Of course, there are more complex collision volumes than simple boxes, and we’ll see in a later tutorial how to enhance collision detection to support any convex shape. Don’t discount the usefulness of simpler shapes like boxes and spheres, though! The calculations to determine collisions between them are generally quite fast, allowing lots of them to be calculated per frame. Also, sometimes we just simply don’t need the additional fidelity that more complex collision detection would bring. Consider the following example of a character picking up a powerup by walking over it:
Does it really matter if we work out exactly which polygon of the powerup was touched by which polygon of the character’s feet? Probably not, so we may as well just model this interaction as a simple box / box intersection test.

As well as knowing if two objects are colliding with each other, we also need to know details on exactly how they are colliding. We need to know roughly which bits of the objects are intersecting each other, so that they can be separated, and by roughly how much they are intersecting (sometimes known as the penetration distance), to calculate the forces that will separate them out again. To help with this, collision detection functions usually don’t just return a true or false answer, but also some additional collision information - in our examples we’ll be determining a collision point (or contact point), and an intersection distance and collision normal.

**Sphere / Sphere Collisions**

Determining whether two spheres have overlapped is fairly easy. If the distance between two spheres is greater than the sum of their radii, they can’t be colliding:

![Sphere Collision Diagram](image)

From this, it is easy to then say that for any two bounding spheres whose distance \(d\) between them is less than the sum of their radii, must be colliding:

![Sphere Collision Diagram](image)

Determining the collision normal \(n\) is similarly easy - it’s just the direction vector between the objects. It’s good to establish a consistent collision normal direction, so we’ll state that if objects \(A\) and \(B\) are colliding, the normal points away from \(A\) and towards \(B\) (the exact normal direction will depend on the collision shape and nature of the intersection, as we’ll see with the other collision types). Finally, the intersection distance \(p\) is simply the difference between the sphere lengths and the sum of their radii.

**AABB / AABB Collisions**

Calculating collisions between axis aligned bounding boxes is a little trickier than with bounding spheres. To determine if they are colliding, we treat them fairly similar to spheres - we calculate the sum of their bounding box dimensions on each axis, and then determine whether the absolute difference in position on each axis is less than the bounding box sum. If all 3 axes are less than their bounding box sum, then the boxes must be colliding. Here’s a few examples to see this in action:
In this first case, we can see that the sum of the $x$ axis box sizes is less than the difference in position on the $x$ axis of the two objects, indicating that maybe there is a collision, here. However, the $y$ axis position difference is greater than the box $y$ axis sizes, so in actuality the boxes are not colliding. Now for case where the objects are colliding:

Now the sum of the AABB sizes on each axis is greater than the relative position between the two objects, indicating that the objects must be in contact. While these examples have only shown 2 dimensions, the same rule stands for 3D, too: the difference in position in all axes must be less than the sum of the box sizes in that axis, or the volumes are not colliding.

While this test tells us if the boxes are colliding or not, it doesn’t really give us the other pieces of the puzzle: the collision normal, the intersection distance, or an intersection point. To get these, we need to do a bit more work. You might initially think that the direction vector between the boxes would be fine for a collision normal, as with bounding spheres, but consider the following example:

Box $a$ should really be pushed straight up slightly to resolve its collision with box $b$, but the direction vector between their origins actually points towards the left, so box $a$ would be pushed slightly to the left, where it will collide again in the next frame if the simulation has gravity pulling it down back towards $b$ - it would end up in a cycle of constantly being shifted leftwards, gaining energy from seemingly nowhere.
To determine a collision normal for two AABBs, we need to think about the penetration distance on each axis individually, and find which axis overlaps the least. Why pick the axis with the least intersection between the objects? Look again at the diagram above - we can visually determine that the two objects are intersecting on the y axis (so object A should really be pushed up, and object B pushed down to ‘fix’ this collision), but their volumes are actually intersecting by far more on the x axis (object A is in fact completely overlapped by object B on this axis). As we go through each axis to see whether the objects intersect on that axis, we can keep track of by how much - if the shapes are determined to overlap, the axis with the least penetration then gives us the collision normal, and the penetration on that axis provides us with our total penetration distance.

The final thing we need is to define a collision point in space, so we know where to apply the forces on our objects to move them apart. It can be seen in the example image above that there’s not any single point in space for some AABB collisions, unlike with sphere/sphere collisions. A later tutorial will cover exactly how to handle cases where there is an area of collision, rather than just a single point, but for now we can determine a valid point by finding the closest point of each shape’s origin inside the other object, and picking one:

![Diagram showing collision points](image)

In some cases though, there’s a problem with this. If we think back to the example of the red box sitting on the blue box, then finding the closest points in each box gives us two quite different points:

![Diagram showing different closest points](image)

In this case, we would expect the closest point on object "B" to be the best choice, as its in the middle of the intersection area, and thus most accurately represents what physically 'should' happen (if the box were traveling straight down, we would expect the response to be for it to bounce back up slightly, not get knocked to the side). So how to choose which point? We will cover the real answer in a later tutorial, but for now, we can use the dot product to determine the best answer. In the above example, we know via the minimum penetration calculation that the y axis is the collision normal. If we take the dot product between the collision normal and the direction between an object’s position and its closest point on the other object, we can see that one of the two points has a ‘closer’ dot product that the other, making it a better candidate for using for a single collision point.

**Box / Sphere Collisions**

Testing collisions between boxes and spheres is much the same as with box intersection tests, in that we find the closest point on the box to the sphere, using the clamp operation, by limiting the sphere’s position to be between the range (box position - box size, box position + size) on each axis. If that point is greater than the radius away from the sphere’s centre, then the objects cannot be colliding! The diagram below should make this clearer:
This lets us know about whether the shapes are colliding, but what about our collision point information? The point itself is simply the closest point on the AABB to the sphere, while the collision normal is the direction vector between the sphere’s origin and the closest point, and the penetration distance can be calculated by calculating the distance from the sphere’s position to the closest point, and subtracting the sphere’s radius:

Collision Detection Considerations

In our simulations, we update our object positions via a series of discrete steps per frame; calculating intersecting objects and separating them out as we go. However, there’s a potential problem with this. Consider the following example of a bullet, moving at a velocity of 10m/s, with a bounding sphere for its collision volume:

At frame A, the bullet was in front of the wall, and at frame B the bullet was behind the wall - This effect is known as tunneling, and is caused due to the bullet traveling so fast there was never a frame where it was intersecting the wall, so no collisions could ever be calculated! For certain types of scenario, this is a pretty serious impairment to the accuracy of our physics simulation, so let’s investigate some ways to solve it (or avoid it altogether!).
Raycasting

The easiest way to avoid this problem specifically for many physics-based interactions in our games is to not treat them as physics objects at all! Many games such as first person shooters and RTS games don’t model bullets as rigid bodies, but simply determine which direction the bullet will go, and then perform a raycast to see what will be hit along this direction. Weapons that perform a raycast for their collision detection rather than rigid body dynamics are often known as *hit scan* weapons - in real life bullets travel in an arc as gravity and wind resistance affects them, but games are usually more about fun than realistic simulation, so an instantaneous, straight line projectile is often fine.

We can extend this concept a little further, too. For something we know will be traveling in a straight line fast (maybe the player picked up a rocket launcher instead of a machine gun?), we could instead raycast from the object, in the direction it is traveling - if the closest object is at a distance of less than the object’s velocity away, we can assume it will hit it, and mark the object for collision next frame at point $p$:

Swept Bounding Volumes

Just performing a raycast is often not enough though - the ray is infinitely thin, but we’re trying to determine the collisions between shapes with volume. We must therefore consider how to make changes to the actual collision volume itself when trying to detect high-speed collisions. Consider the bullet going through the wall example from earlier. In both frames A and B, the collision volume of the bullet was not large enough to intersect with that of the wall, but in reality we know that they must have collided. To solve this, we could ‘stretch’ the bounding volume of an object as it moves, so that it encapsulates both its point at time A, and at time B, like so:

This is known as a *swept* bounding volume. If we then detect a collision with the swept volume, then at some point between frame time A and B, a collision occurred. We can determine approximately *when* using the collision point on to the collided object (in this case, the wall), using a raycast:
We know the object’s position both before and after the collision, so we can form a ray which starts at the 'before' point, and aims in the direction of the 'after' point. We also know the distance between those positions, and also the distance between the raycast origin and the intersection point, the ratio between those two, multiplied by \(dt\), will let us know how far in to the physics update the collision occurred. Why would we need the approximate collision time? Wouldn’t just moving our bullet to the collision point, and then resolving the collision as normal work? For a collision against a static object it would be fine, but consider this example:

Now we have two high speed objects! If we sweep both of their volumes, it appears that there would be a collision, but did they really? To solve this, we need to determine when between frame A and frame B that object A collided with the swept volume of B, and from that time, determine where object B was, and then perform an additional collision detection test at these new positions, using the object’s 'true' collision volumes (in our bullet example, we’re assuming this is a bounding sphere).

This should be enough to determine with reasonable accuracy whether or not two shapes collide over a time period - remember, a physics system will run often multiple times per frame, and we aim to run at perhaps 60FPS, meaning that every iteration of our physics system may only be 2 or 3 milliseconds in length, making most swept volumes quite small.
A final note on swept bounding volumes - the method you use to stretch the volume matters a great deal to the accuracy of the simulation. You might first think that for AABBs and spheres, that just stretching them so that they now encompass the end point is enough, but take a look at these examples:

That’s a pretty big sphere! While it’s certainly expanded to cover the end point, it’s also stretched out to take up space that the object will never fill during the course of its movement between frame A and frame B. This could generate false collisions, or at the very least, cause additional collision tests that take up your frame time computing. Instead, we must be smarter with our swept volumes - an AABB becomes a swept OOBB, and a sphere becomes a swept capsule:

A capsule can be thought of as a cylinder with half a sphere on each end, and is usually defined as using a height, and a radius, like so:

Capsules are useful beyond just sweeping volumes. They are often used as the basic collision model of a player character, as the rounded edge provides a more accurate fit against the character’s head.
versus a box, and the rounded bottom can be used as a more accurate representation of where the character may intersecting with ramps and steps:

Detecting collisions in a simulation

We now know the formulas for determining whether various simple shapes are intersecting with each other, and what data we’ll later use to resolve this collisions. But we currently don’t really know how to determine when to use these collision detection methods. As it’s possible for objects to move around the world, it’s therefore possible that any object could be colliding with any other object in the world at any given moment in time. Therefore, in code, to detect our collisions and resolve them, we can do something like this:

```
for every object x in game world {
    for every object y in game world {
        if (IsColliding(x, y)) {
            ResolveCollision(x, y)
        }
    }
}
```

Seems simple enough, but there’s a problem - it’s slow! There’s a nested set of for loops, each of which has to go over every object in the world; to put it another way, we must do $N^2$ operations to detect all our collisions. That quickly builds up to a lot of collision detection tests! Imagine you were making a racing game where 100 cars competed to travel across the country; even ignoring any collisions with other cars that may be on the road, that’s 10,000 collision detection tests that must be performed every frame.

In the above code example, we’ll end up testing whether object x is colliding with object y, AND if object y is colliding with object x - as far as our physics interactions go, that’s the same test, so really we should avoid repeating it. Even more stupidly, in cases where $x == y$, we’d be testing whether an object is colliding with itself! We can adjust our for loop to something a bit more sensible, like so:

```
for int x = 0; x < lastObject; ++x {
    for int y = x + 1; y < lastObject; ++y) {
        if (IsColliding(x, y)) {
           ResolveCollision(x, y)
        }
    }
}
```

In this case, our inner for loop will skip any test combination that’s already been done (looking at the ints created by the loops, they will now never generate object pair (6,5) or (6,6), but will still
form (5,6)). The loop itself is still characterised by $O(N^2)$ as the number of potential collisions still increases, but we save some time, and save some potential headaches that might occur if collision resolution was pushing objects multiple times in a frame, and thus potentially adding too much energy into our physics system.

We’ll see in a later tutorial that we can use properties about our knowledge of the world to skip collision testing between objects that can’t possibly be colliding, but for now we’ll just deal with the ‘slow’ way.

**Tutorial Code**

To show off collision detection and response, we’re going to once again modify the test scene we’ve been building up. As well as being able to click on objects to push them around, we’ll also be able to receive some feedback on when those objects have collided. By pressing the gravity button, we’ll also be able to see the objects be pulled down and bounce onto the floor, rather than just go through it.

**CollisionDetection Namespace Changes**

To detect collisions between our shapes, we need some new functions! So far we’ve been introduced to AABBs and spheres, so we’ll need at least 3 new functions (to handle AABB vs AABB collisions, sphere vs sphere collisions, and AABB vs sphere collisions). As well as these, we’re going to further split up AABB tests, so that we get the true/false collision answer from one function, but the actual collision data from another - this is something that will help us out in a later tutorial. Finally we need a function which takes in a pair of GameObjects, and calls the correct intersection function to apply. We also need a struct, to hold the collision information, so that we can resolve the collision correctly in the next tutorial.

These methods to perform all of these operations have been declared within the CollisionDetection namespace, but as in the raycasting tutorial, they’re currently empty - we’ll be filling in each to see how the theory outlined earlier translates to a practical implementation. In these methods, we’re going to be filling in a struct we haven’t so far come across, CollisionInfo, which looks like this:

```c
struct ContactPoint {
    Vector3 position;
    Vector3 normal;
    float penetration;
};

struct CollisionInfo {
    GameObject* a;
    GameObject* b;
    ContactPoint point;
    void AddContactPoint(Vector3 position, Vector3 normal, float p){
        point.position = position;
        point.normal = normal;
        point.penetration = p;
    }
};
```

**CollisionDetection namespace additions**

It might at first seem strange that we are splitting up the concept of an individual contact point (with its associated position, normal, and penetration amount), from the overall concept of a collision between a pair of objects, but we’ll see in a later tutorial how we may sometimes have multiple collision points between a pair of objects (we’ve already tangentially discussed some of the reasons as to why this may be!).
The first function we’ll implement is \textit{ObjectIntersection}; it’s currently a defined function that does nothing except return false, so we’ll need to fill it out with some actual logic. The purpose of this function is to take in two of our \textit{GameObjects}, and determine which of the collision detection functions to use. There’s a variety of ways in which this could be implemented (virtual functions, double dispatch, function pointers, and so on), but to make it obvious what is going on, we’ll take a direct approach and use \textbf{if} statements. We’ll start the method by getting pointers to the collision volumes of our objects (lines 3 and 4), and if one shape doesn’t have a volume, return false straight away, as they can’t possibly collide with anything (line 7). If the objects can collide, we fill in the start of our \textit{CollisionInfo} struct with the two objects, and get the object’s transforms (lines 13 and 14 - we don’t strictly need to do this, but it cuts down on repeated calls to the same methods).

```cpp
bool CollisionDetection::ObjectIntersection(  
    GameObject* a, GameObject* b, CollisionInfo& collisionInfo) {
    const CollisionVolume* volA = a->GetBoundingVolume();
    const CollisionVolume* volB = b->GetBoundingVolume();

    if (!volA || !volB) {
        return false;
    }

    collisionInfo.a = a;
    collisionInfo.b = b;

    const Transform& transformA = a->GetConstTransform();
    const Transform& transformB = b->GetConstTransform();

    VolumeType pairType = (VolumeType)((int)volA->type | (int)volB->type);

    if (pairType == VolumeType::AABB) {
        return AABBIntersection((AABBVolume&)*volA, transformA,  
                               (AABBVolume&)*volB, transformB, collisionInfo);
    }

    if (pairType == VolumeType::Sphere) {
        return SphereIntersection((SphereVolume&)*volA, transformA,  
                                (SphereVolume&)*volB, transformB, collisionInfo);
    }
```

Next, we need to send our objects, and the \textit{collisionInfo} struct, off to the correct function to detect the possible collision. To do this, we’re going to do a little bit of bitwise operations on the object’s types. This is an \textbf{enum} (\textit{VolumeType}, defined in \textit{BoundingVolume.h}). As each entry in the \textit{VolumeType} enum is a power of two (so only one bit is set), if we do a bitwise OR of both object’s types, we get a bitmask of the type of collision. If after the bitwise OR the type still equates exactly to either AABB (value of 1) or Sphere (value of 2), then it means that \textit{both} shapes must be the same type, and so their ordering doesn’t really matter. On line 15 we perform the bitwise OR (with the \textbf{|} symbol), and then use \textbf{ifs} to either return the result of an AABB intersection, or a Sphere intersection on the objects. In each of these cases, we need to cast the collision volume to the correct type:

```cpp
VolumeType pairType = (VolumeType)((int)volA->type | (int)volB->type);

if (pairType == VolumeType::AABB) {
    return AABBIntersection((AABBVolume&)*volA, transformA,  
                            (AABBVolume&)*volB, transformB, collisionInfo);
}

if (pairType == VolumeType::Sphere) {
    return SphereIntersection((SphereVolume&)*volA, transformA,  
                            (SphereVolume&)*volB, transformB, collisionInfo);
}
```

But what to do if the objects being tested \textbf{aren’t} of the same type? We could do some bit shifting when we create the \textit{pairType} variable to differentiate between cases where object \textit{b} is a sphere versus when \textit{a} is a sphere and test against that, but for now we’ll just handle the two cases we could get so far:
if (volA->type == VolumeType::AABB &&
    volB->type == VolumeType::Sphere) {
    return AABBSphereIntersection((AABBVolume&)*volA, transformA,
                                (SphereVolume&)*volB, transformB, collisionInfo);
}
if (volA->type == VolumeType::Sphere &&
    volB->type == VolumeType::AABB) {
    collisionInfo.a = b;
    collisionInfo.b = a;
    return AABBSphereIntersection((AABBVolume&)*volB, transformB,
                                (SphereVolume&)*volA, transformA, collisionInfo);
}

return false;

CollisionDetection::ObjectIntersection Function

Note that we might need to swap the objects of our collisionInfo variable around, to match up to the order of the parameters the function expects - AABBSphereIntersection always takes in the AABB volume object first, so we flip them in the collisionInfo struct to reflect this (lines 33 and 34).

Implementing Sphere-Sphere collision detection

With the selection of a collision detection function completed, we can start implementing the actual detection functions. The easiest to follow is sphere-sphere collisions, so we’ll start there. Find the currently empty SphereIntersection function within the CollisionDetection namespace, and add in the following code:

```
bool CollisionDetection::SphereIntersection(
    const SphereVolume& volumeA, const Transform& worldTransformA,
    const SphereVolume& volumeB, const Transform& worldTransformB,
    CollisionInfo& collisionInfo) {

    float radii = volumeA.GetRadius() + volumeB.GetRadius();
    Vector3 delta = worldTransformB.GetWorldPosition() -
                   worldTransformA.GetWorldPosition();

    float deltaLength = delta.Length();

    if (deltaLength < radii) {
        float penetration = (radii - deltaLength);
        Vector3 normal = delta.Normalised();
        Vector3 collisionPoint = collisionPoint =
                                 worldTransformA.GetWorldPosition() +
                                 (normal * (volumeA.GetRadius() - (penetration * 0.5f))) ;
        collisionInfo.AddContactPoint(collisionPoint, normal, penetration);
        return true;//we’re colliding!
    }
    return false;
}
```

CollisionDetection::SphereIntersection Function

This matches up pretty well to the theory outlined earlier. We get the sum of the two object’s radii (line 6), then work out the distance between the two object’s positions (line 7 and 10). If the distance between them is less than the sum of their radii, they must be intersecting (line 12), and so we can work out the penetration distance (the sum of the radii, minus the distance between the objects), the
collision normal (the direction vector between the two objects), and a collision point - in this case we’re travelling along the collision normal from object a, and stopping short of the object’s radius by half the penetration distance (we’re splitting the difference between the two objects, basically). If the distance is larger than the sum of the radii, we can’t be colliding, and so return false (line 22).

Implementing AABB-Sphere collision detection

Sphere-sphere is pretty easy, but going through it allowed us to see how the collisionInfo struct should be filled in. Now we can make things a little more advanced, and look at AABB-sphere collision detection, using the currently empty AABBSphereIntersection function. As described earlier, the core of AABB-sphere intersection is to find the closest point on the box to the sphere’s location. We can do this by simply clamping the relative position of the sphere, to limit it to the box size - for any axis where the position is greater than the box size, we ‘lock’ it to the box size. We can do that in code by getting the box dimensions (line 5) and the relative position of the sphere to the box (line 7), and then forming a new position in space, closestPointOnBox (line 10). To clamp a value to a range, we can use the Clamp function inside the Maths namespace, which takes in a value a, along with a minimum and maximum, and returns a modified a that is limited to the range passed in (for example Clamp(10,3,12) will try to limit the value 10 to be between 3 and 12, and so will return 10, as it lies within the range, but Clamp(20,3,12) will return 12, as 20 is beyond the maximum value allowed).

```cpp
bool CollisionDetection::AABBSphereIntersection(
  const AABBVolume & volumeA, const Transform & worldTransformA,
  const SphereVolume & volumeB, const Transform & worldTransformB,
  CollisionInfo & collisionInfo) {
  Vector3 boxSize = volumeA.GetHalfDimensions();
  Vector3 delta = worldTransformB.GetWorldPosition() -
      worldTransformA.GetWorldPosition();
  CollisionDetection::AABBSphereIntersection Function
  Vector3 closestPointOnBox = Maths::Clamp(delta, -boxSize, boxSize);

  Vector3 localPoint = delta - closestPointOnBox;
  float distance = (localPoint).Length();
  if (distance < volumeB.GetRadius()) {// yes, we’re colliding!
    collisionInfo.AddContactPoint(
      closestPointOnBox,
      distance == 0.0f ? delta.Normalised():localPoint.Normalised(),
      (volumeB.GetRadius() - distance)
    );
    return true;
  }
  return false;
}
```

CollisionDetection::AABBSphereIntersection Function

Once we have the sphere’s closest point on the box, we can determine how far away the sphere is from this point, by subtracting this point from the sphere’s relative position (line 11). If this point lies at a distance less than the sphere’s radius (line 14), then it must be colliding, and we can fill in our collisionInfo struct. The collision point will be the closest point on the box to the sphere, and the penetration distance will be the sphere’s radius, minus the distance from the sphere to the box point. For the collision normal, we can use the direction vector from the box position to the sphere’s closest point (line 17). Note that we’re also checking to see if the distance has become zero. Why? In cases where the sphere’s origin is inside the box, we get a distance of 0.0 (in these cases, the clamping operation won’t change any of the values, and thus closestPointOnBox will equal the same value as delta, and so subtracting one from the other gives us a vector of zero length).
Implementing AABB-AABB collision detection

The AABB-AABB collision detection has been split up into two functions - one to tell us whether the objects are colliding, and one to fill in the collision information. The easier to understand is the testing function, so we’ll start off by implementing it inside the `AABBTest` function:

```cpp
bool CollisionDetection::AABBTest(
    const Vector3& posA, const Vector3& posB,
    const Vector3& halfSizeA, const Vector3& halfSizeB) {
    Vector3 delta = posB - posA;
    Vector3 totalSize = halfSizeA + halfSizeB;
    if (abs(delta.x) < totalSize.x &&
        abs(delta.y) < totalSize.y &&
        abs(delta.z) < totalSize.z) {
        return true;
    }
    return false;
}
```

CollisionDetection::AABBTest Function

It’s logic follows the earlier description of AABB intersection - we’re looking to see if the distance between the object’s on each axis is less than the sum of the box sizes on that axis, and only if that is true for all axes should we consider the objects intersecting. On line 4 we work out the distance on each axis, and line 5 we calculate the sum of the box sizes, and then on line 7 we calculate whether the distances are less than the box sizes. We need to use the abs function to get the absolute value of the relative position, as the box A might be to the left of box B, or to the right - it doesn’t matter, all we care about is whether the difference is position is greater than the box dimensions.

After the `AABBTest` function, you should be able to find an empty `AABBIntersection` function, too. We’ll start adding some code to it to make it actually do something:

```cpp
bool CollisionDetection::AABBIntersection(
    const AABBVolume& volumeA, const Transform& worldTransformA,
    const AABBVolume& volumeB, const Transform& worldTransformB,
    CollisionInfo& collisionInfo) {
    Vector3 boxAPos = worldTransformA.GetWorldPosition();
    Vector3 boxBPos = worldTransformB.GetWorldPosition();
    Vector3 boxASize = volumeA.GetHalfDimensions();
    Vector3 boxBSize = volumeB.GetHalfDimensions();
    bool overlap = AABBTest(boxAPos, boxBPos, boxASize, boxBSize);
    if (overlap) {
        static const Vector3 faces[6] =
            { Vector3(-1, 0, 0), Vector3( 1, 0, 0),
              Vector3( 0, -1, 0), Vector3( 0, 1, 0),
              Vector3( 0, 0, -1), Vector3( 0, 0, 1),
            };
    }
}
```

CollisionDetection::AABBIntersection Function

It’s a pretty simple start - we extract the positions and sizes of the AABBs, and feed them into the `AABBTest` function to determine whether they are overlapping. If they are overlapping, things get a bit more interesting, as the next bit of code to add to this new function demonstrates:
Vector3 maxA = boxAPos + boxASize;
Vector3 minA = boxAPos - boxASize;
Vector3 maxB = boxBPos + boxBSize;
Vector3 minB = boxBPos - boxBSize;

float distances[6] =
{
  (maxB.x - minA.x), // distance of box 'b' to 'left' of 'a'.
  (maxA.x - minB.x), // distance of box 'b' to 'right' of 'a'.
  (maxB.y - minA.y), // distance of box 'b' to 'bottom' of 'a'.
  (maxA.y - minB.y), // distance of box 'b' to 'top' of 'a'.
  (maxB.z - minA.z), // distance of box 'b' to 'far' of 'a'.
  (maxA.z - minB.z)  // distance of box 'b' to 'near' of 'a'.
};

float penetration = FLT_MAX;
Vector3 axis;

for (int i = 0; i < 6; i++)
{
  if (distances[i] < penetration) {
    penetration = distances[i];
    axis = faces[i];
  }
}

CollisionDetection::AABBIntersection Function

As the theory outlined earlier, we need the axis of minimum penetration between the two objects. To determine this, and help determine the collision normal, there’s quite a lot to go through. From a box’s world position, we can determine the minimum and maximum position for each axis by either adding or subtracting the box’s size. On lines 21 to 25 we calculate this, and use it to calculate the amount of overlap on each axis - the maximum extent of object b, minus the minimum extent of object a on each axis gives us the amount of overlap (to put it another way, we’re seeing how far into box a, that box b’s maximum position extends). We then iterate through these penetration extents (line 40), and work out which is the smallest value, storing the penetration, and the axis (from the static faces array, which is arranged to match up to the distances array) every time we find a smaller value - this is why the penetration float starts with the maximum value a float can hold, rather than starting at 0.

Once we’ve iterated through all the possible penetration amounts and found the best, we can then start to build the collision info. Finish off the AABBIntersection function by adding the following code:

Vector3 closestPointOnBoxA = Maths::Clamp(boxBPos, minA, maxA);
Vector3 closestPointOnBoxB = Maths::Clamp(boxAPos, minB, maxB);
Vector3 aDir = (boxAPos - closestPointOnBoxB).Normalised();
Vector3 bDir = (boxBPos - closestPointOnBoxA).Normalised();
float aDot = Vector3::Dot(aDir, axis);
float bDot = Vector3::Dot(bDir, axis);
if (abs(aDot) > abs(bDot)) {
  collisionInfo.AddContactPoint(
    closestPointOnBoxB, axis, penetration);
}
else {
  collisionInfo.AddContactPoint(
CollisionDetection::AABBIntersection Function

Here we are working out which of the two potential collision points is closest to matching up to the origin of the box along the collision normal, as shown back on page 4 - by finding the 'best' collision, we're more likely to get stable results later on, when we start actually resolving the collisions.

PhysicsSystem Class Changes

Nearly all of the complex code was added in the CollisionDetection namespace, so there’s not much to do. First off, we need to create a way of determining whether collisions are occurring each frame, as outlined earlier. To do this, the PhysicsSystem class has a BasicCollisionDetection method, but once again it has been left empty. Add in the following code:

```cpp
void PhysicsSystem::BasicCollisionDetection() {
    std::vector<GameObject*>::const_iterator first;
    std::vector<GameObject*>::const_iterator last;
    gameWorld.GetObjectIterators(first, last);

    for (auto i = first; i != last; ++i) {
        if ((*i)->GetPhysicsObject() == nullptr) {
            continue;
        }
        for (auto j = i + 1; j != last; ++j) {
            if ((*j)->GetPhysicsObject() == nullptr) {
                continue;
            }
            CollisionDetection::CollisionInfo info;
            if (CollisionDetection::ObjectIntersection(*i, *j, info)) {
                std::cout << "Collision between " << (*i)->GetName()
                            << " and " << (*j)->GetName() << std::endl;
                info.framesLeft = numCollisionFrames;
                allCollisions.insert(info);
            }
        }
    }
}
```

PhysicsSystem::BasicCollisionDetection Method

It’s not so different to how we did raycasting, except now instead of iterating over all of the objects once (via the iterators we get from the GameWorld class on lines 2-4), we need to go over the objects twice. The important thing to get right here is line 10 - we are starting the inner for loop at one element past the outer for loop, so that we don’t resolve identical collisions multiple times in a frame. As we might be inserting objects into the game world that don’t have physics objects, we also need to skip over these (a little bush or flower may have a graphical representation, but no physical representation, for instance). For now, we’re going to just output that a collision has taken place into the console, but we’ll soon be adding some code to actually resolve the collision to this method, too. The if statement on line 15 calls our new VolumeIntersection method, which will return true if a collision has taken place, and if so will fill in the info struct with the appropriate data for later use.

There’s one last thing we do, which is to insert the successfully detected collision into an STL::List,
which will let us keep track of objects that are colliding - later on we might need to use this information across multiple frames.

As an example of why we might want to keep a list of colliding objects, we’re going to look at another currently empty function, `UpdateCollisionList`. This gets called by the `PhysicsSystem` every frame, and should have the following code in it:

```cpp
1 void PhysicsSystem::UpdateCollisionList () {
2   for (std::set<CollisionDetection::CollisionInfo>::iterator i =
3       allCollisions.begin(); i != allCollisions.end(); ) {
4     if ((*i).framesLeft == numCollisionFrames) {
5       i->a->OnCollisionBegin(i->b);
6       i->b->OnCollisionBegin(i->a);
7     }
8     (*i).framesLeft = (*i).framesLeft - 1;
9     if ((*i).framesLeft < 0) {
10       i->a->OnCollisionEnd(i->b);
11       i->b->OnCollisionEnd(i->a);
12       i = allCollisions.erase(i);
13     }
14     else {
15       ++i;
16     }
17   }
}
```

**PhysicsSystem::UpdateCollisionList Method**

What is it doing? Games without any feedback from the physics system as to which collisions have occurred aren’t very exciting - we need to know when a rocket has hit a player to reduce their health, or when they have dropped the companion cube into the furnace in *Portal*. So in this function, we’re going to go through the list of collisions we filled up in the `BasicCollisionDetection` method, and if they’re brand new to the list this frame, call a `virtual` function on the `GameObjects` contained within the `CollisionInfo` struct - by default this won’t do anything, but it allows for subclasses of the `GameObject` to implement game specific logic by overriding the `OnCollisionBegin` method. Sometimes, we might even need to know when an object has stopped colliding with something (maybe the player has wandered into some lava, and should lose health until they leave), so in this case we can detect it and call another `virtual` function `OnCollisionEnd`. Otherwise, we reduce a counter on each collision pair, and if necessary, update the iterator or remove the pair from the list - later on we’ll see why we need to keep objects around for multiple frames. Every time the same object pair collides, this counter gets reset (by reinserting it in the `BasicCollisionDetection` method), so only if a pair of objects hasn’t been colliding with each other for a while will the `OnCollisionEnd` method be called.

That’s everything for now! If we use the mouse pointer to push objects together like we did in previous tutorials, the objects will still overlap (we aren’t *resolving* the collision, merely *detecting* it), but we should be able to see in the console that a collision is occurring, allowing us to test that our spheres and boxes return the correct collision state.

**Conclusion**

Collision detection is an important part of any physics engine, as without them we can’t determine how objects should interact with each other - objects will fall through the floor due to gravity, and powerups will be impossible to pick up! Being able to efficiently detect that collisions are occurring between the shapes in our world is therefore incredibly important, and thus tutorial has shown enough to get us started in building up all of the collision detection we need. In the next tutorial, we’ll take a look at how to resolve the collisions we’re detecting, allowing our objects to bounce around the world, and come to rest on the ground.
Further Work

1) As well as outputting a string to the console to represent when a collision has occurred,

2) While the tutorial text has discussed capsules, and how they might be useful, we haven’t yet seen any code to implement them. Try making a \texttt{CapsuleCollider} class that inherits from \texttt{CollisionVolume}, and which uses a new \texttt{VolumeType enum} to identify it. Remember that we need a height variable, and a radius to represent our shape - treating the ends as spheres and the middle like an AABB is a good place to start, but you may also wish to think about projecting a collision volume’s position onto a plane.

3) If you do add capsules, you might then want to think about adding the ability to \textit{sweep} a bounding volume - just try it with spheres for now, and test it by firing spheres at high speed towards a very thin wall; you should be able to create a scenario where the spheres will sometimes bounce through, unless swept spheres are used.