

# Explorations at the Interface of Social Epidemiology and Complex Systems: A Theoretical Health Inequality Model (THIM)

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& Reed Beall



***\*\*Special thanks to Steve Gribble, George Kaplan and the NIH-funded Network for Inequality, Complexity and Health\*\****

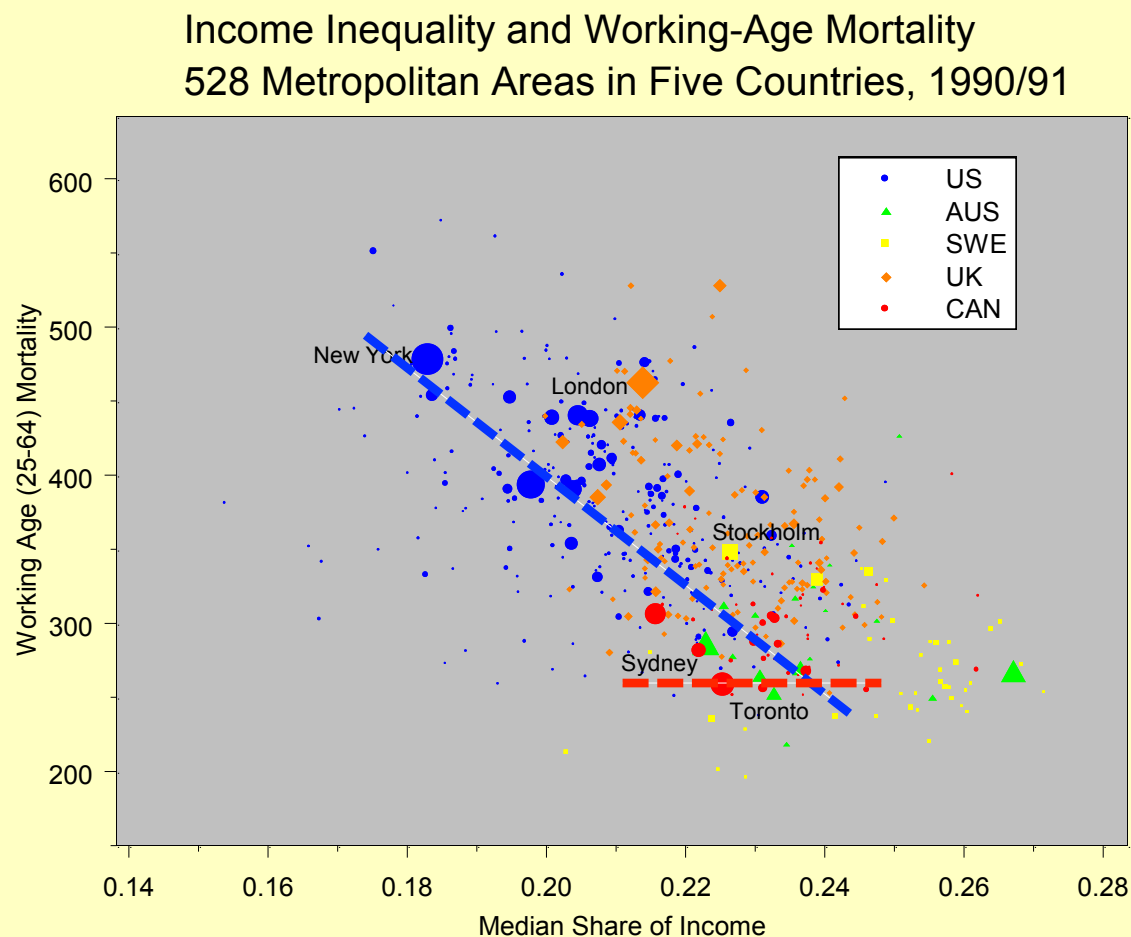
# Contrasting income inequality & mortality association in US vs Canada



Nancy Ross et al's  
1991 results

Median share income  
indicator

- higher inequality = lower median share = smaller share of income going to the bottom 50% of the population

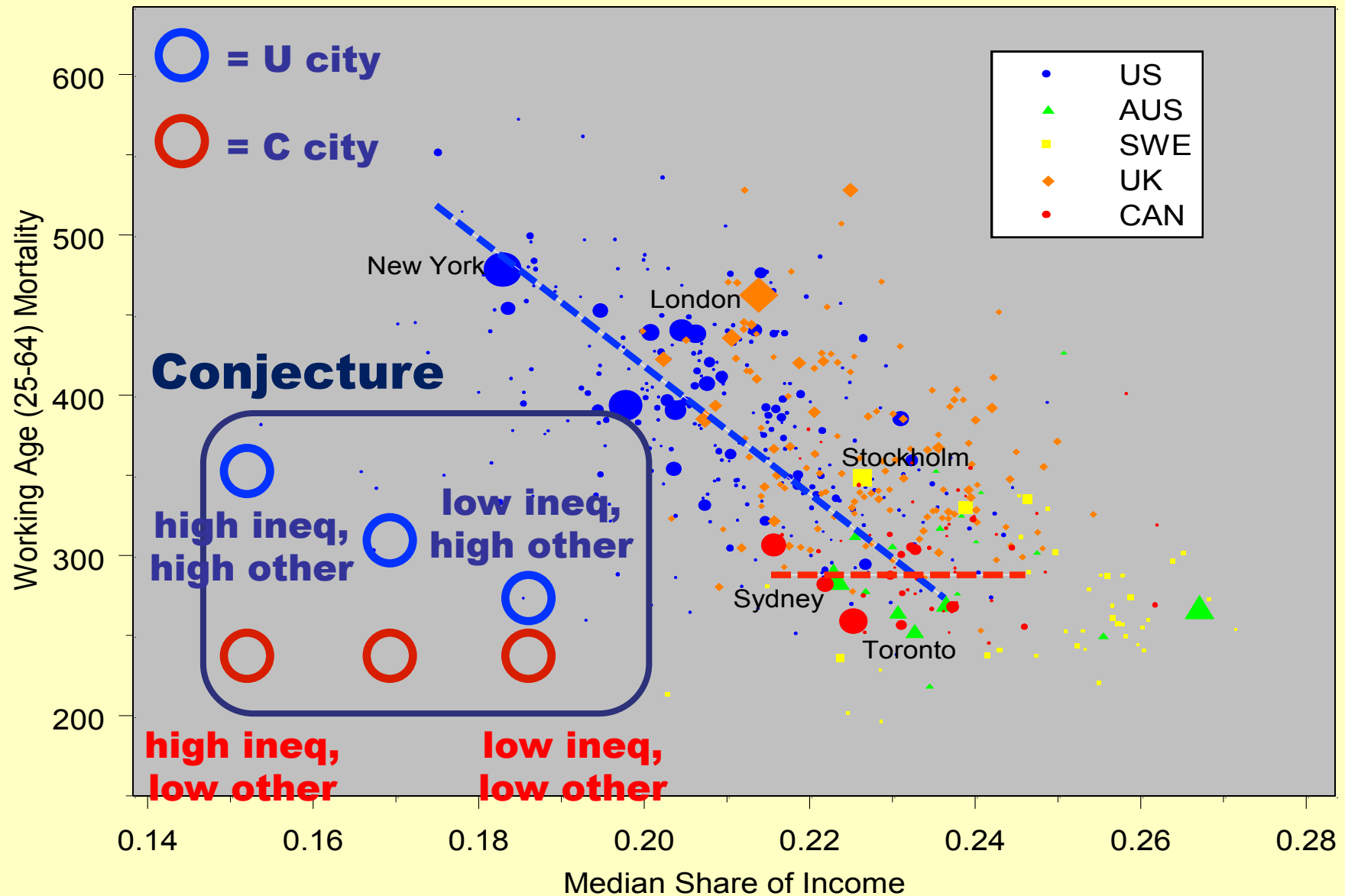


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REVES, Edinburgh, May 2014  
Slide - 2

# Income Inequality and Working-Age Mortality

## 528 Metropolitan Areas in Five Countries, 1990/91



# Formulate Explanation/Theory & Model Selection



- Main factors to consider
  - overall level of income inequality
  - neighbourhood income segregation
  - parental + neighbourhood influences on children's education / subsequent incomes
  - “returns to education” in terms of future income
  - effects of income on health and mortality

# Build Theory: Constructing an Agent-Based Model (ABM)



- Model needs to capture main factors
  - *individual heterogeneity* in income and health
  - parental influences, life course  $\Rightarrow$  *trajectories*
  - neighbourhood (nbhd) factors: education as a major pathway + nbhd sorting  $\Rightarrow$  *multi-level*
- Abstraction (i.e. major simplification) is essential
- Model should reflect “stylized facts”
  - i.e. as simple as possible, but not too simple
- Open to “emergent” phenomena

# Some Building Blocks of THIM city



## Main agent ("sim") variables:

a = age of the agent = uni-sex "sim"; max a = 100.

Time = measured in "years" (say)

H = health status, a QALY index in the [0,1] interval.

D = dead (Boolean, true or false).

Y = income (dollars, non-negative).

E = "education" measured in years, integer in [1, 20]

L = location in a "city" comprised of many (e.g. 50) nbhds

## Multi-level variables (critical component to our conjecture!):

individual agents / families (parent-child dyads) /

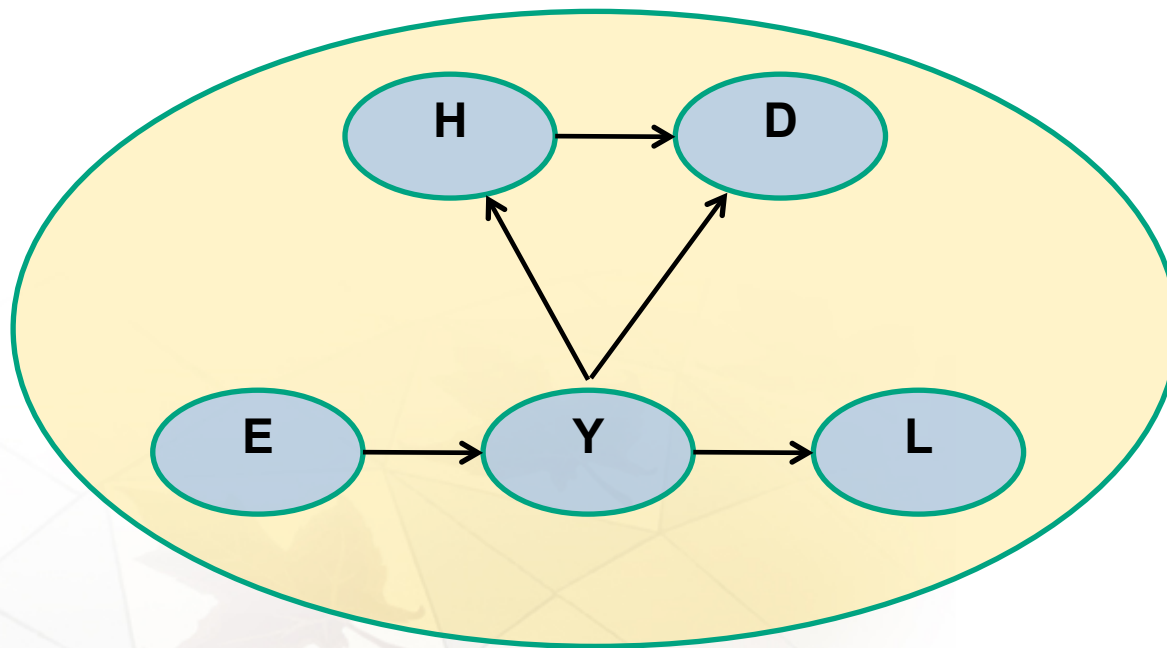
neighbourhoods (nbhds) / cities



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# THIM: “Web of Causality” at Individual “Sim” Level

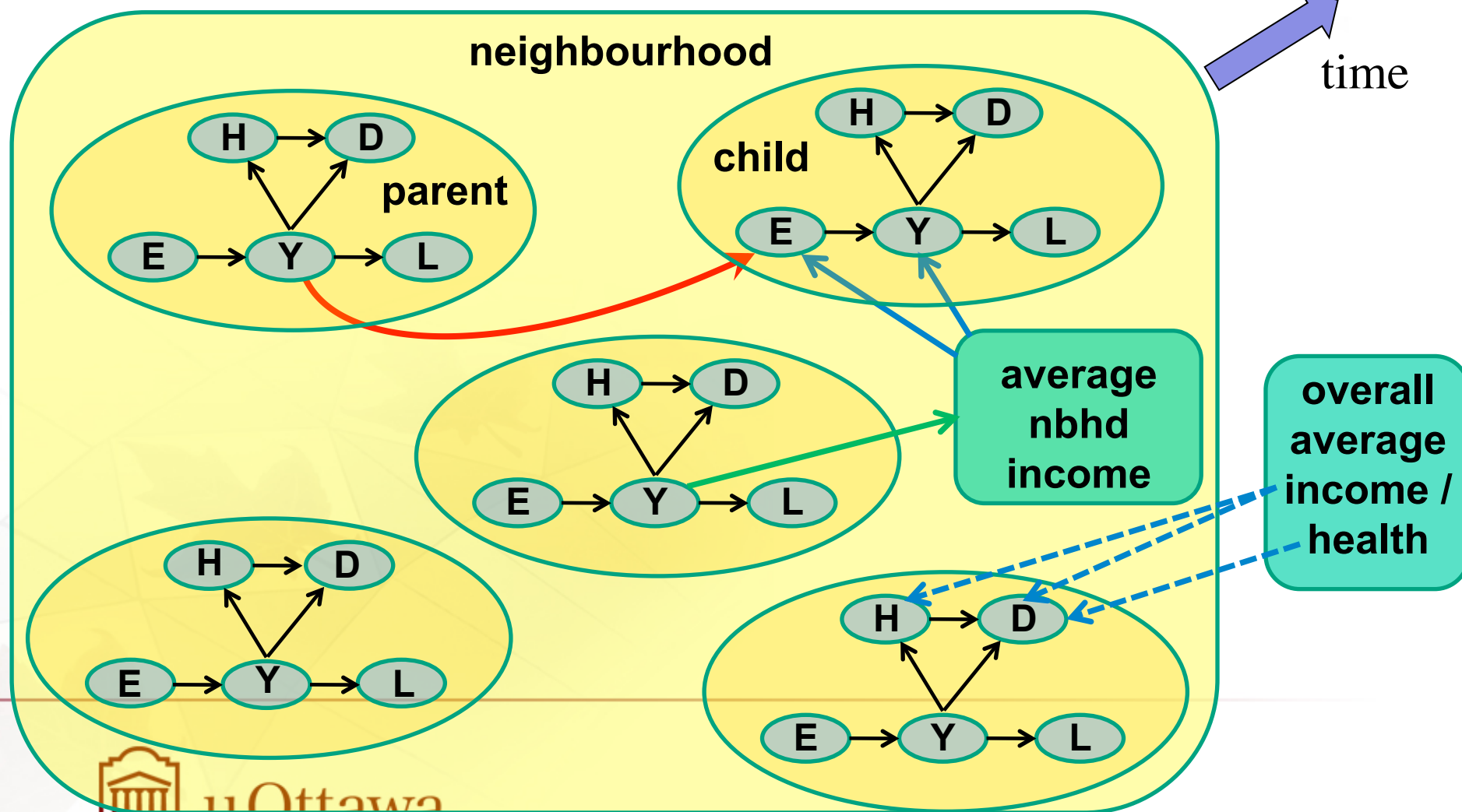


## Building Blocks

- E = education
- Y = income
- H = health
- D = death
- L = location

# THIM – Multi-Level Relationships:

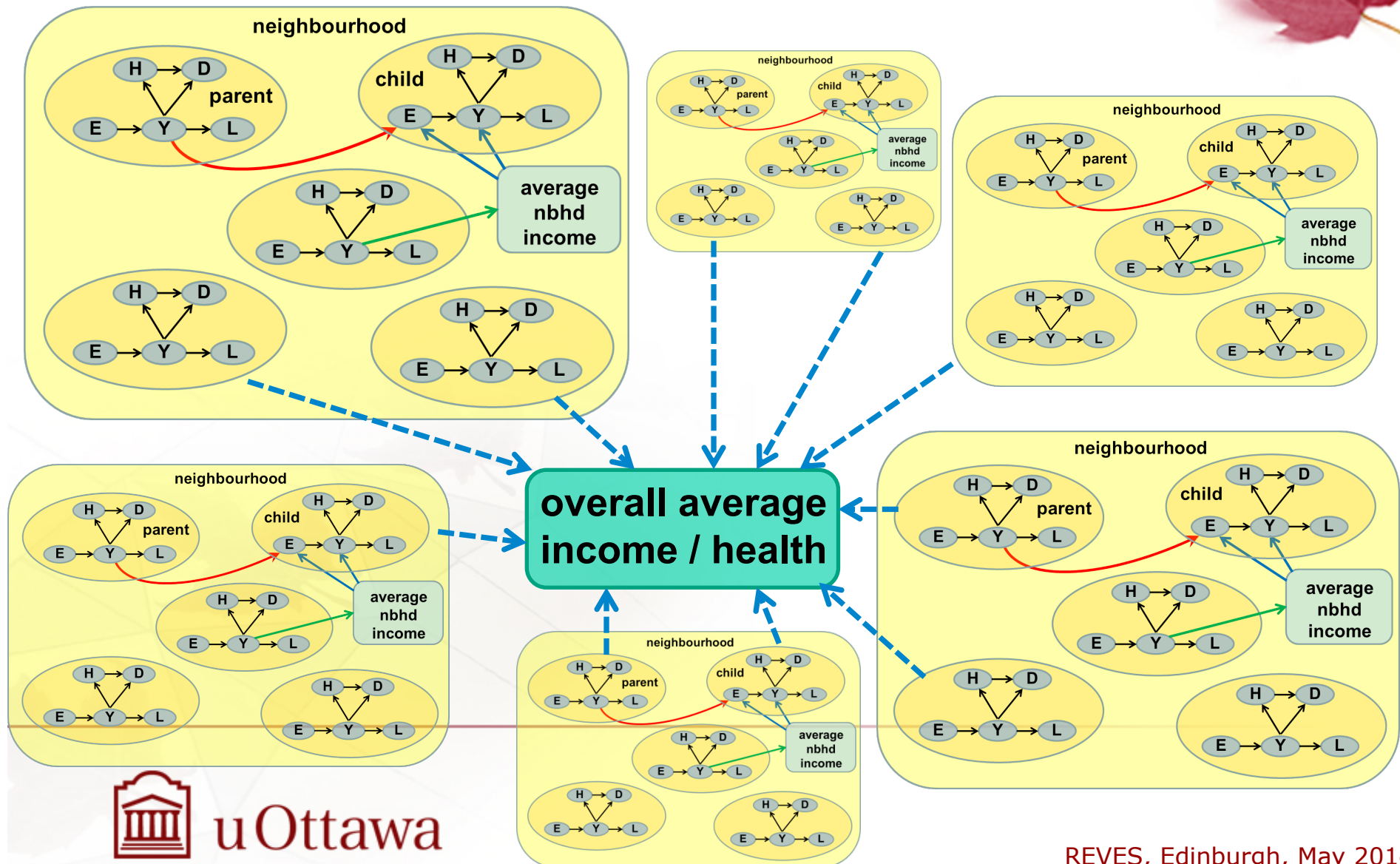
Individual sims -> Parent-child dyads <-> nbhd





# THIM: Many Nbhds = "City"

## *City-wide Factors*



# THIM Equations

- *colour = level of aggregation*
- *multiple levels increases complexity*

Fixed at birth:

education (E) = fcn (parent's income, average nbhd income, symmetric randomness)

potential income ( $Y^*$ ) = fcn (education, parent's income, average nbhd income, skewed randomness)

Evolving over time / age:

income (Y) = average income for given age x individual's potential income ( $Y^*$ ) x skewed randomness

change in health (H) = random drift (mostly down) + fcn (own income relative to those at similar ages)

mortality risk (D) = average mortality rate for given age x fcn (own income relative to those at similar ages, own health relative to the overall average)

nbhd mobility ( $\Delta L$ ) = fcn (own income, own nbhd average income, other nbhds' average incomes)

# Review Data & Stylized Facts to Tailor Simulation Parameters



Data literature review for stylized facts of C and U cities. Some examples...

- OECD PISA studies
- OECD Skills Outlook 2013
- Miles Corak's "Great Gatsby Curve." See Journal of Economic Perspectives, Volume 27, No. 3, 2013

Conclusions from review of stylized facts for simulation parameters. U cities have...

- much higher income sorting by nbhd and more ndhds
- 50% higher parental income impact on child's education and income
- higher impact of nbhd average income on children's education and income
- stronger link between own income and mortality

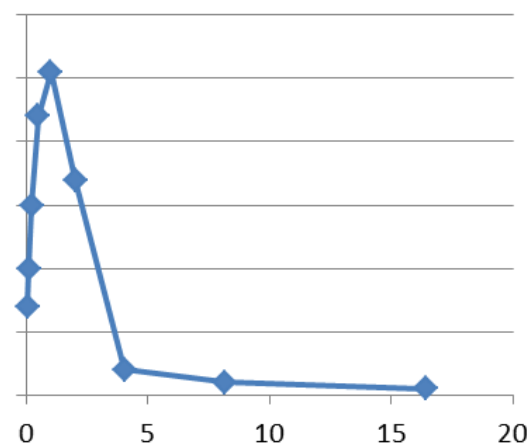
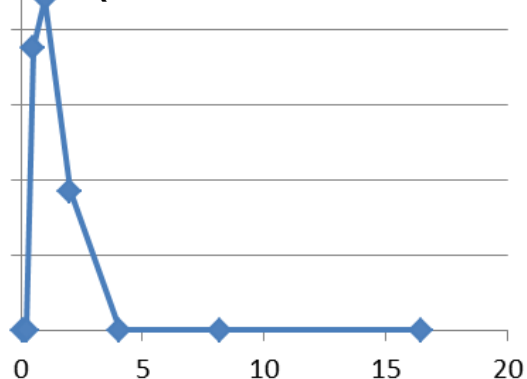
Simulation experiment set up

- Simulation for a wide range of overall "potential" income inequality levels
- focus on LE and HALE as health outcomes
- questions: are the U cities less healthy than the C cities, and is the slope for U cities steeper?

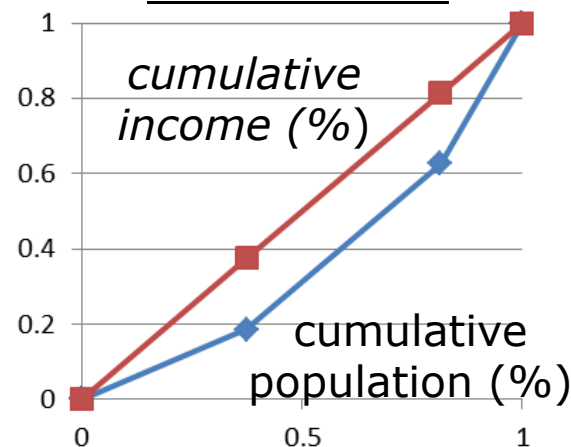
# Input Parameters: High/Low Inequality “Potential (Y\*) Income” Distributions



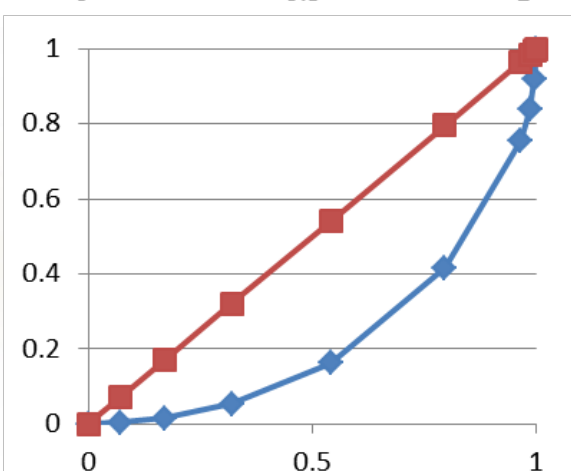
Income Densities  
(scaled so mean = 1)



Lorenz curves



Low Inequality;  
Gini = 0.271



High Inequality;  
Gini = 0.534



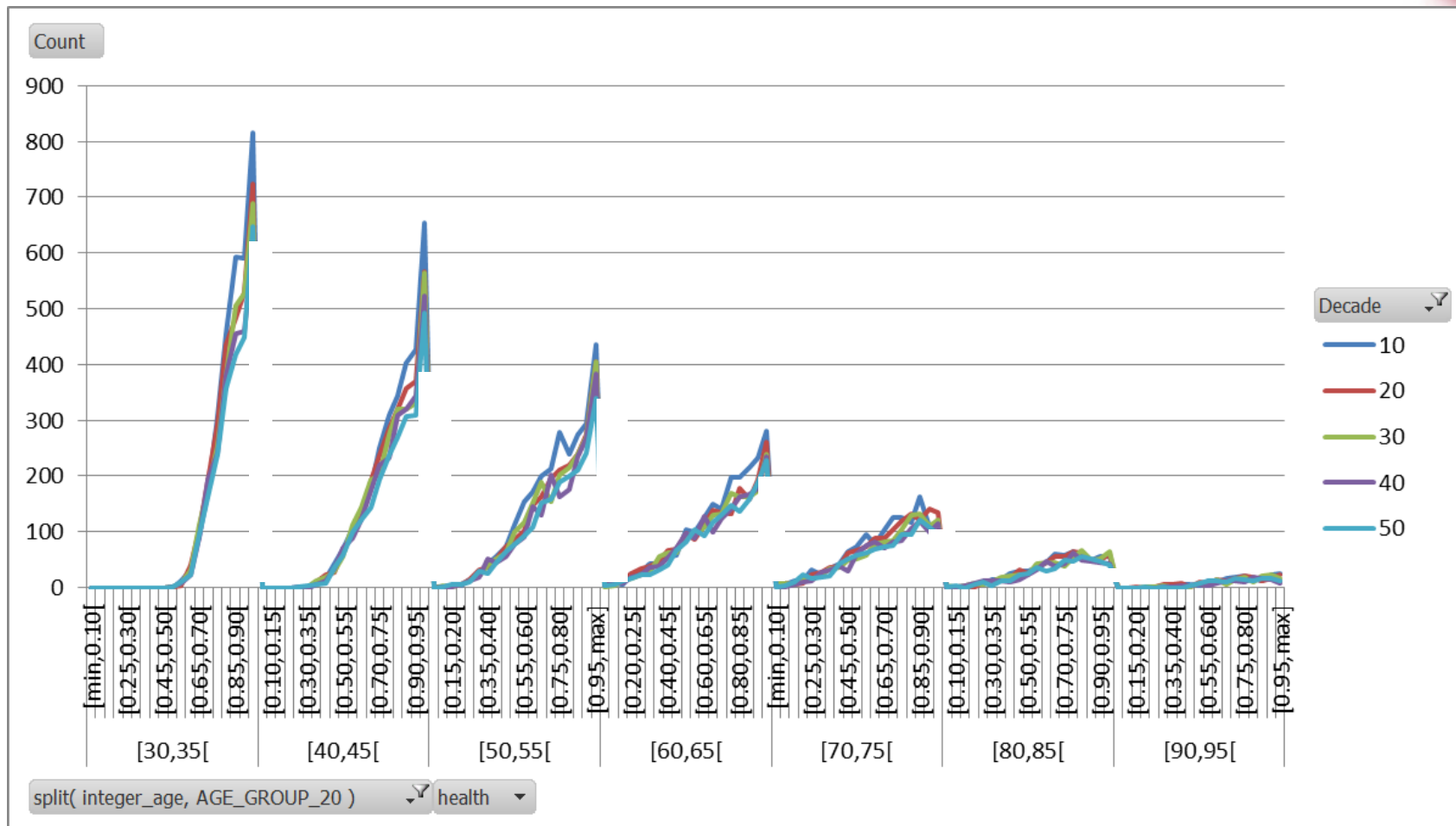
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# “Validating” THIM outputs



- THIM is a theoretical model  $\Rightarrow$  conventional validation is not appropriate
- look for verisimilitude instead
- especially “emergent” outputs = those outputs not directly connected to inputs, i.e. resulting from the interactions of many inputs

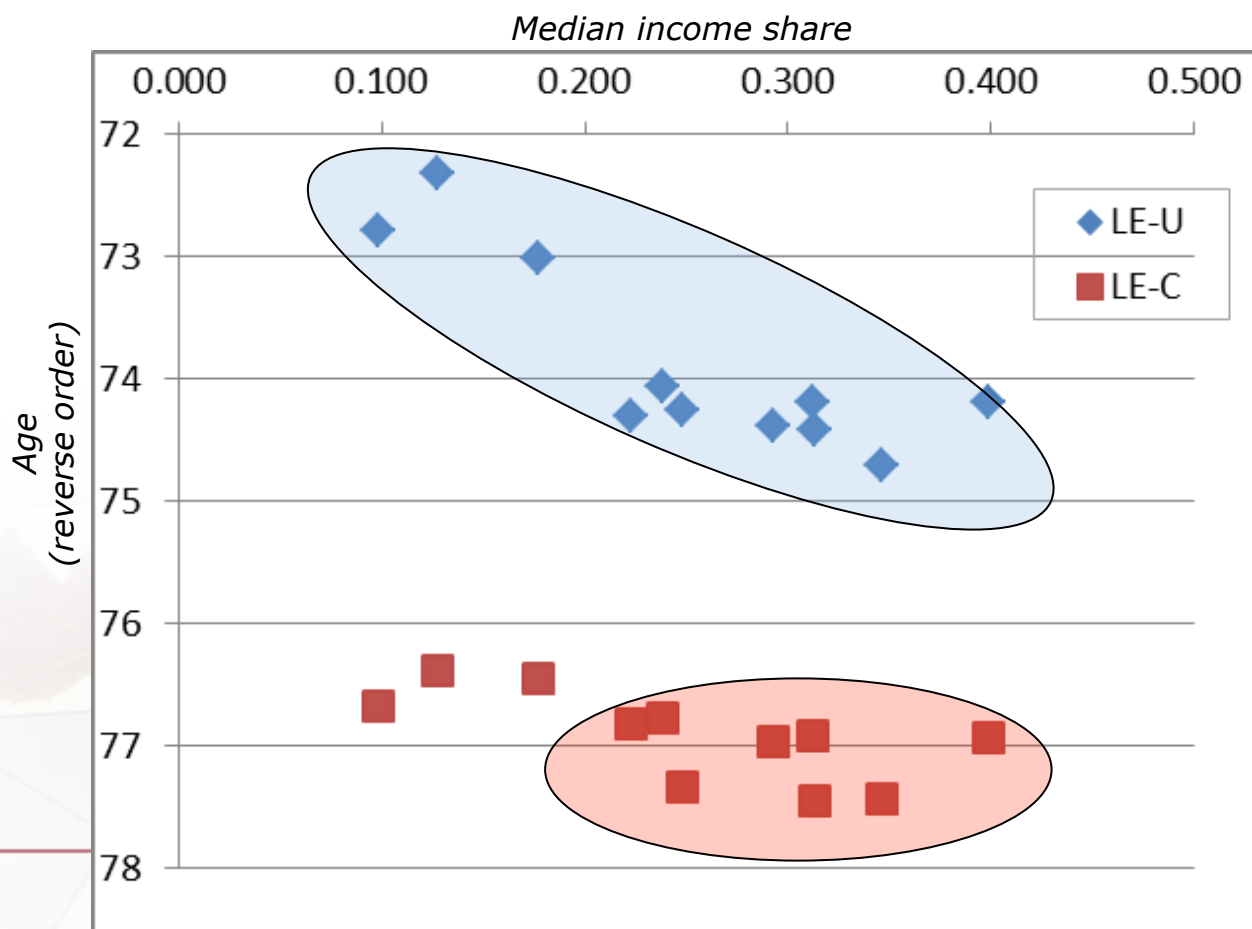
# Simulated Health Distributions Within Each Selected 5 Year Age Group



# LE and HALE Outputs for **City U (blue)** & **City C (red)** and Income Inequality



LE outputs from THIM



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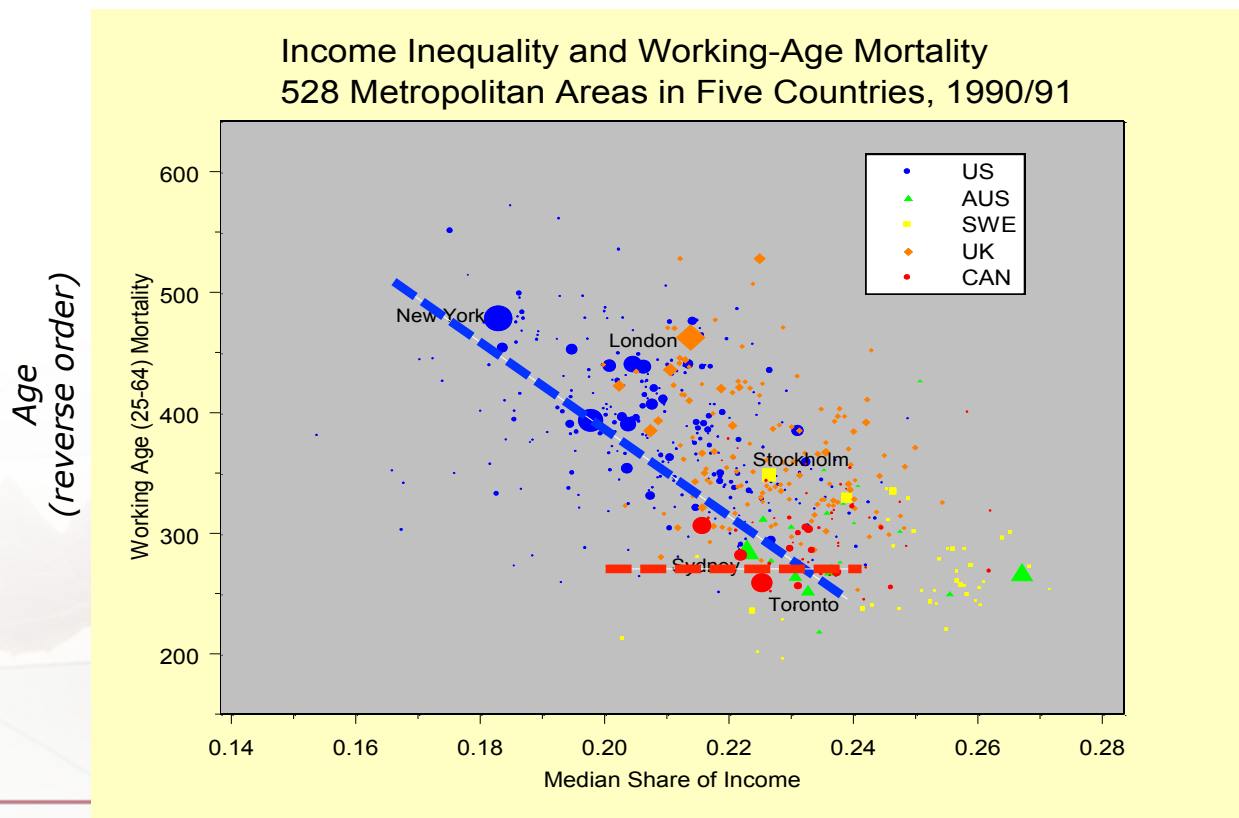


# LE and HALE Outputs for **City U (blue)** & **City C (red)** and Income Inequality



## Ross et al Results

*Median income share*



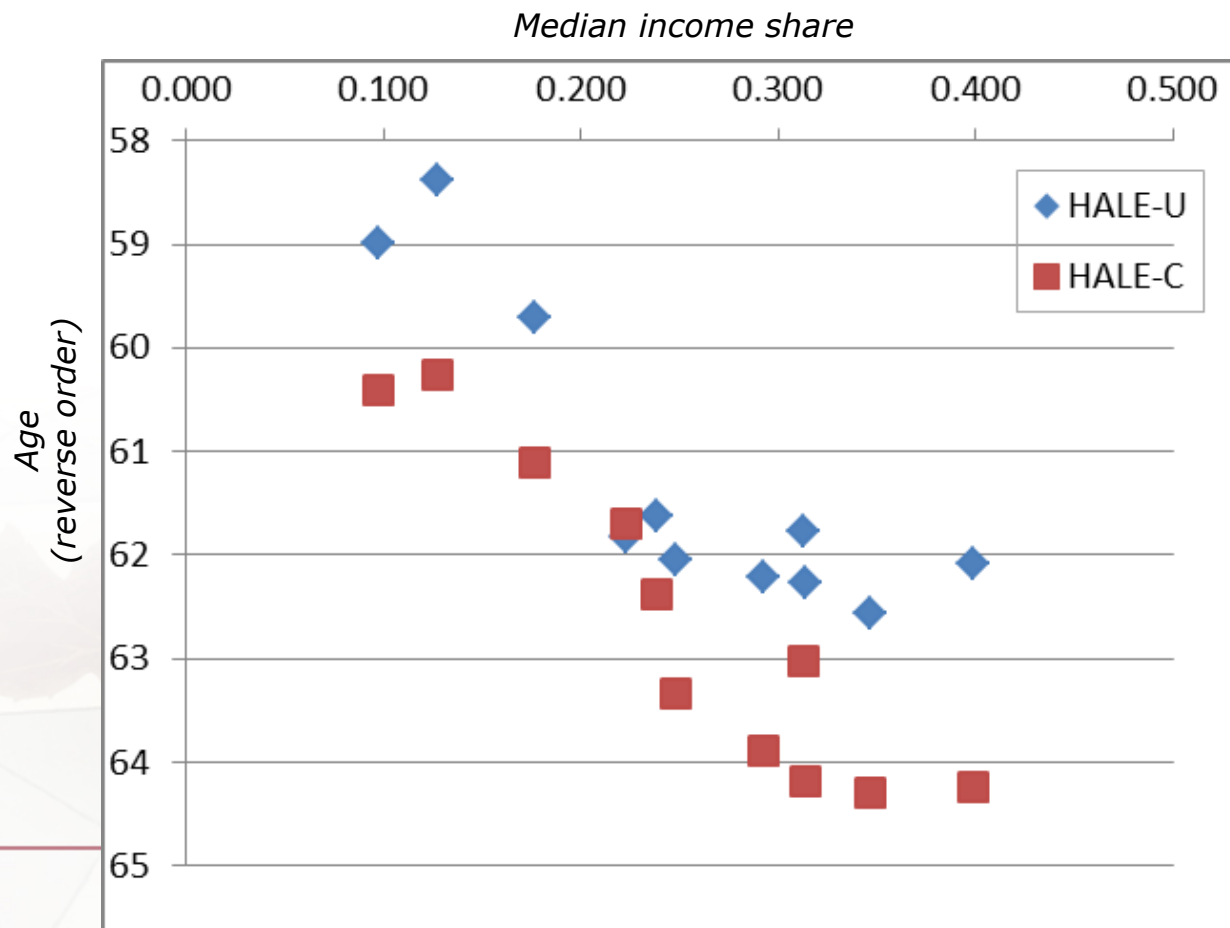
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# LE and HALE Outputs for **City U (blue)** & **City C (red)** and Income Inequality



## HALE outputs from THIM



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# THIM – Concluding Comments



- the realities of individual heterogeneity (including ubiquitous skewedness) + multiple interacting levels of influence (individual  $\leftrightarrow$  parent  $\leftrightarrow$  nbhd  $\leftrightarrow$  city)  $\Rightarrow$  agent-based / complex systems simulation models are needed
- “realistic” behaviours can be generated from a rather simple (albeit complex systems) model
- some Canada-US differences in the (ecological = city) income inequality-mortality relationship, so far, can and others cannot be “explained” by the factors and parameter values tested
- further explorations with THIM plus better internationally comparable data are needed

# Questions, Comments & Discussion

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# Extra Slides Placeholder



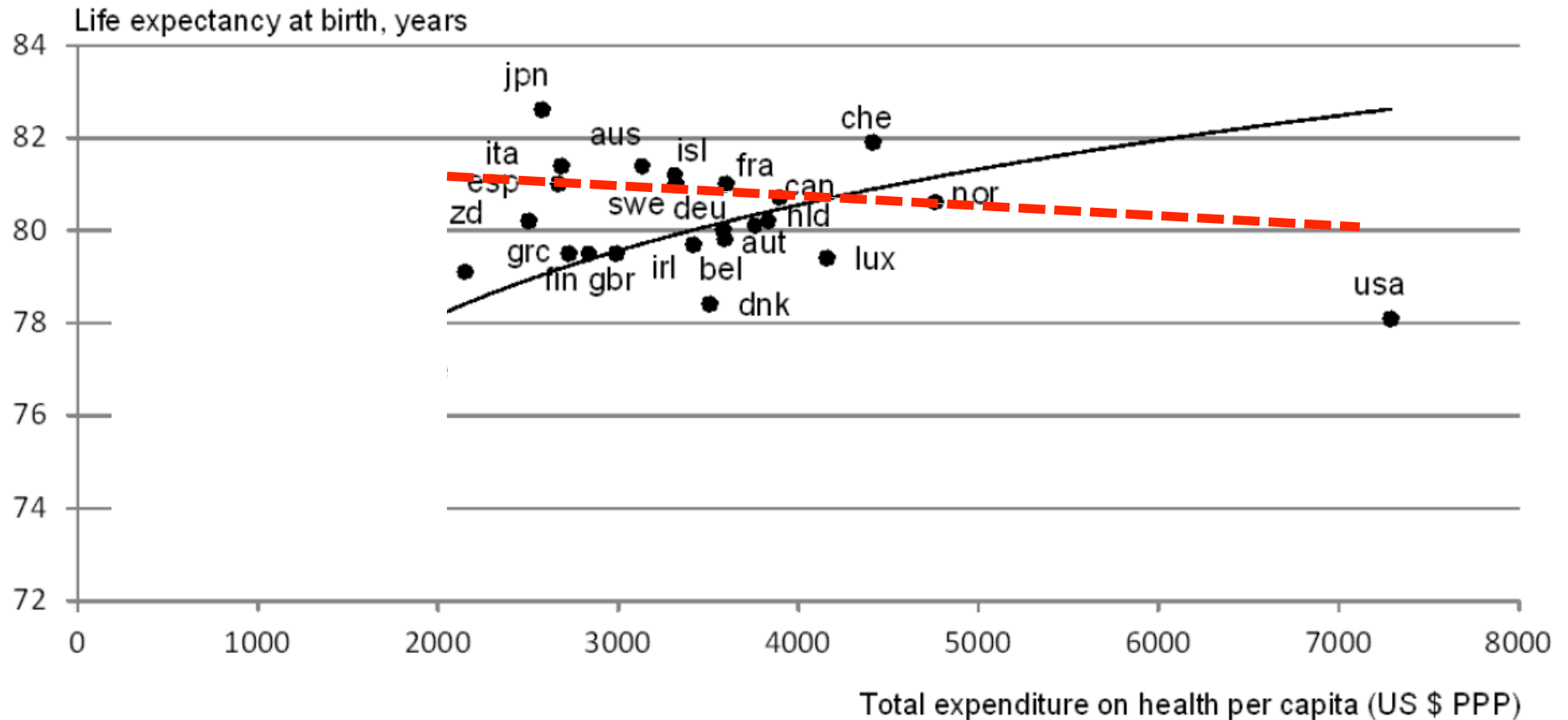
# On stylized facts...



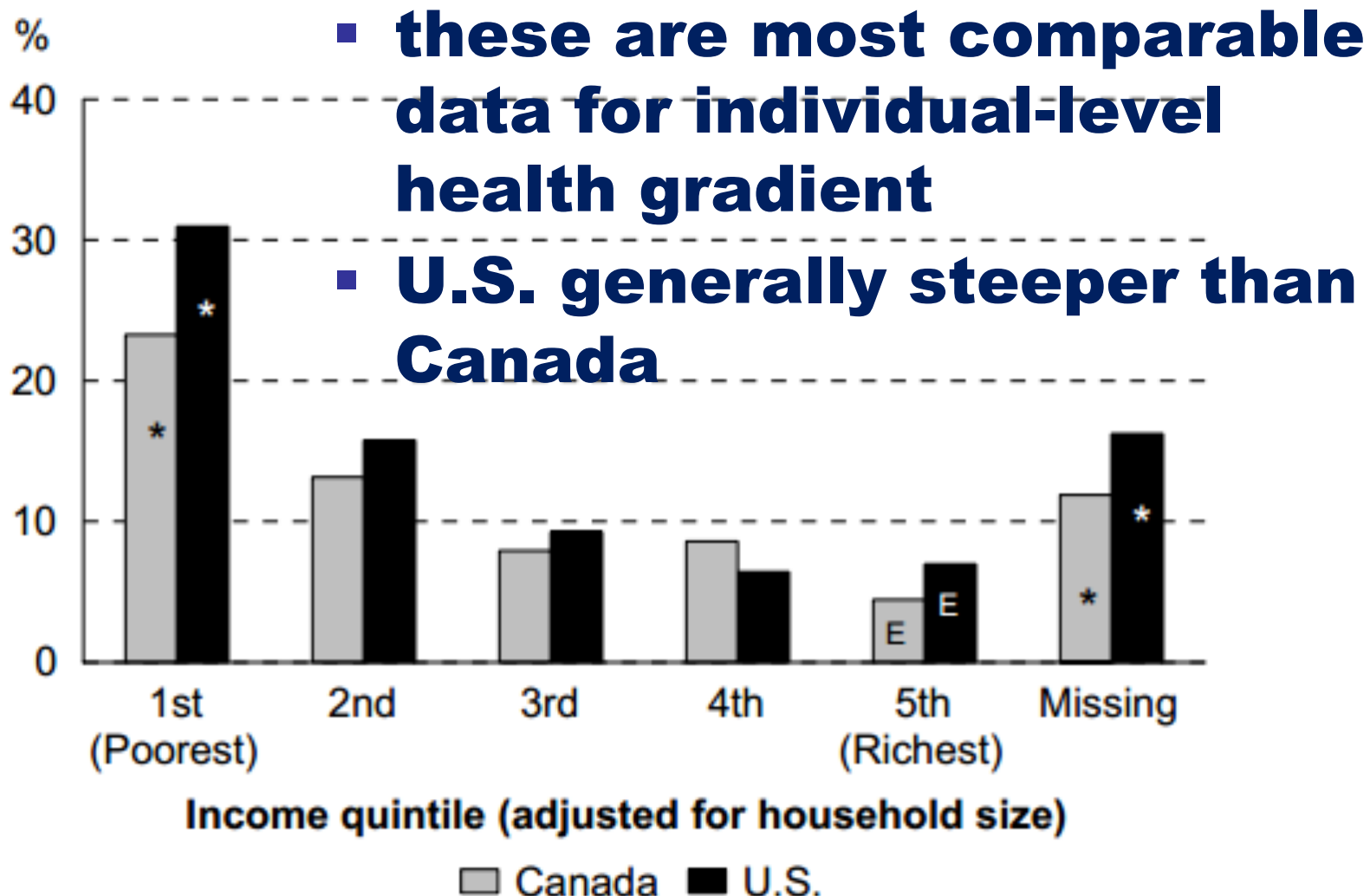
# OECD 2010 – Health Care Expenditure Per Capita versus Life Expectancy

## Health Care (input) $\neq$ Health

Joumard, I., C. André and C. Nicq (2010), “Health Care Systems: Efficiency and Institutions”, *OECD Economics Department Working Papers*, No. 769, OECD Publishing.  
doi: 10.1787/5kmfp51f5f9t-en



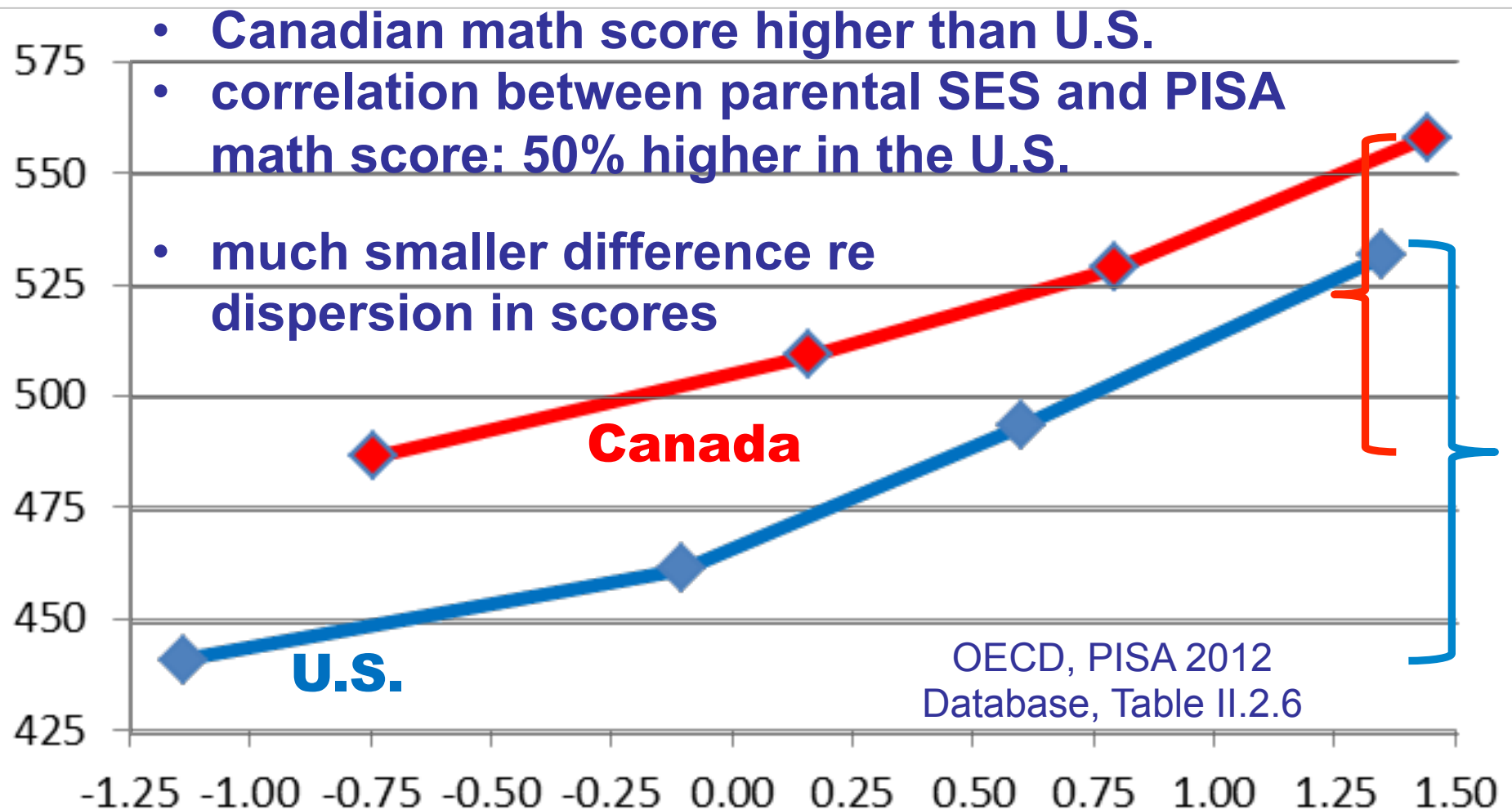
Fair/poor general health by household income quintile, Canada and United States, 2002/03<sup>‡</sup>



*Data source: Joint Canada/United States Survey of Health, 2002/03.*

*Notes: Household population aged 18 and over.*

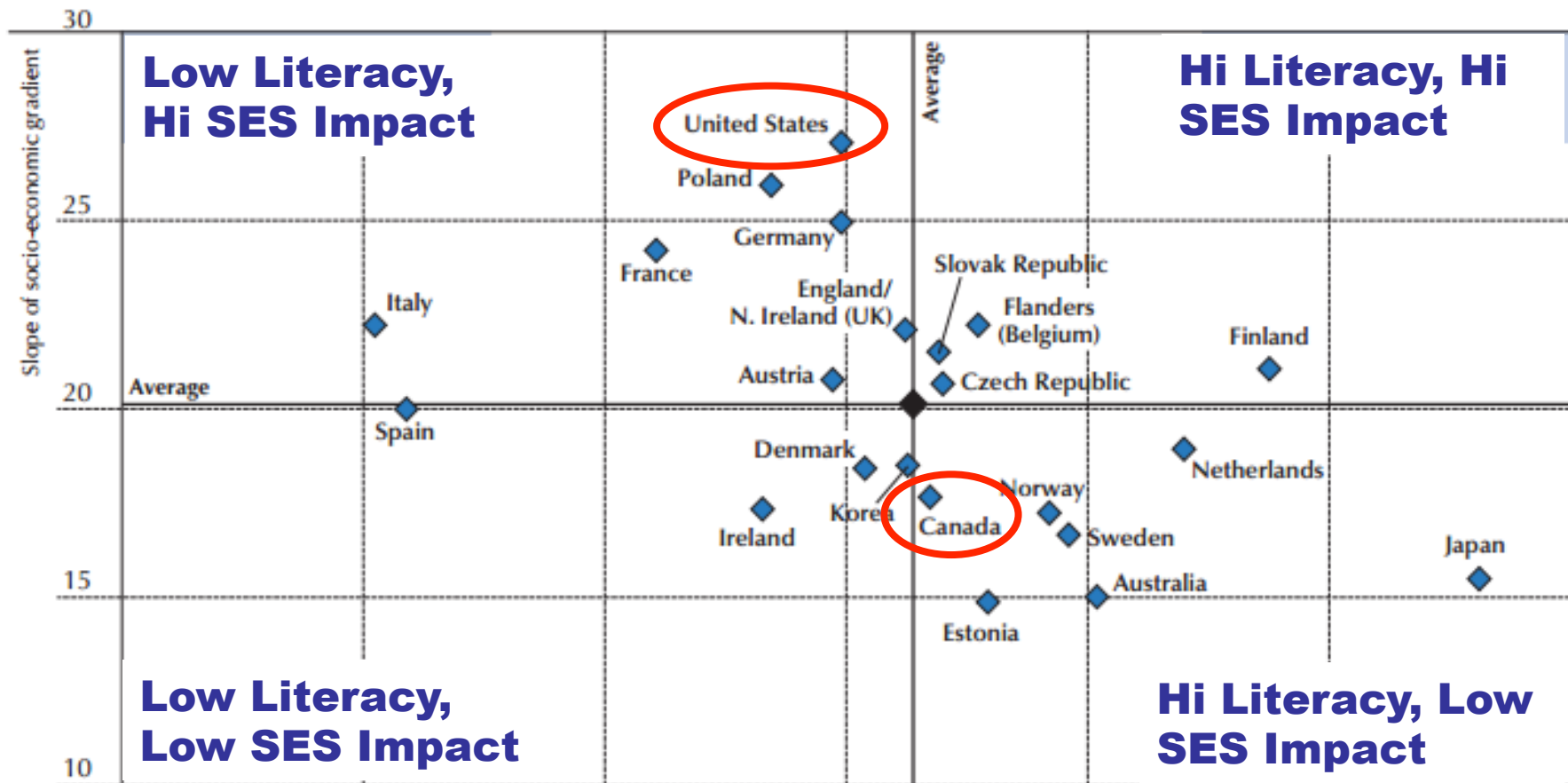
# Parental Influence – PISA Math Scores by Parental Socio-Economic Status (SES) Quartiles, OECD 2013





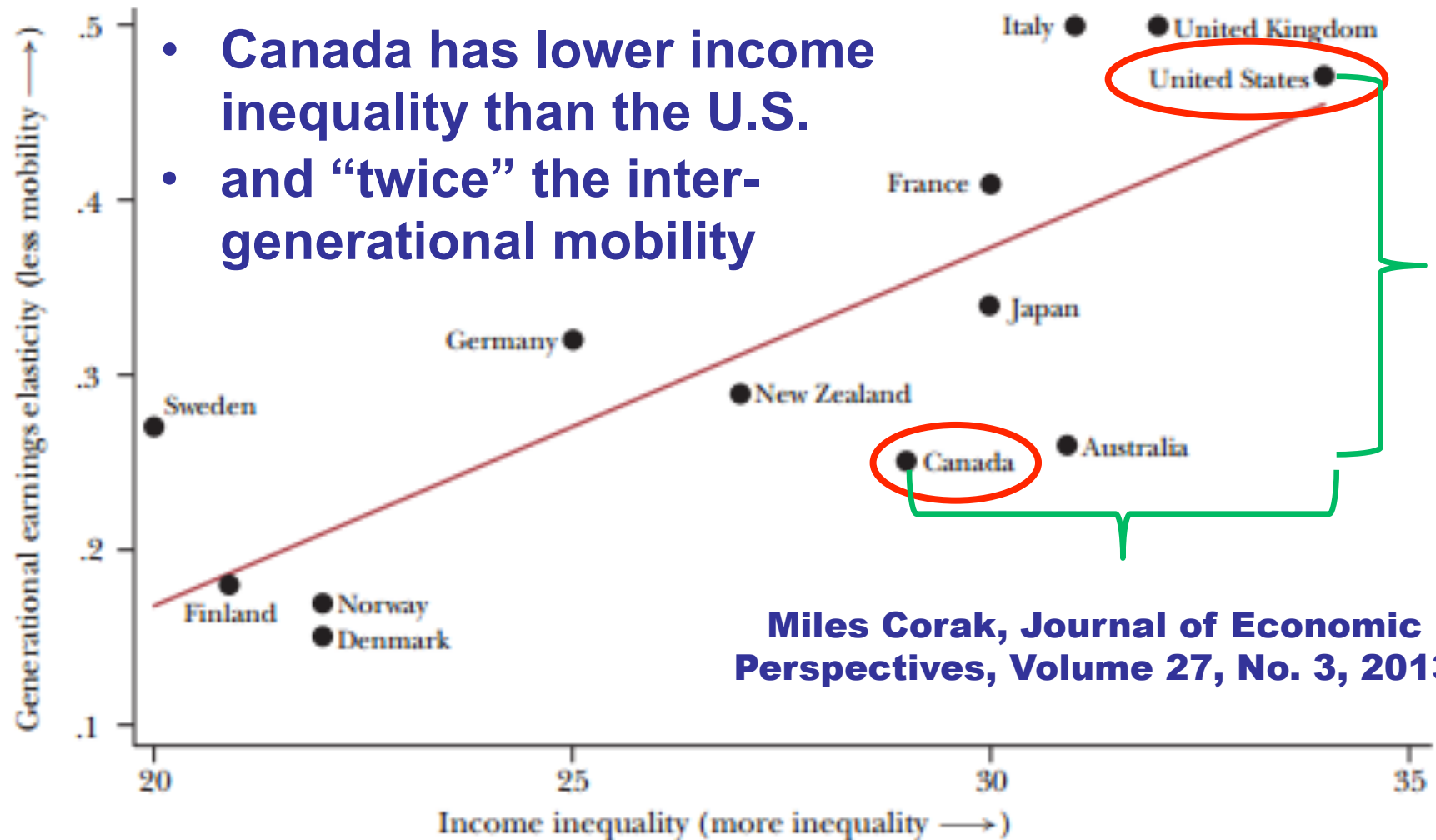
# Parental Influence – Adult Literacy Score by Slope of SES Gradient

(OECD Skills Outlook 2013 Figure 3.8c)



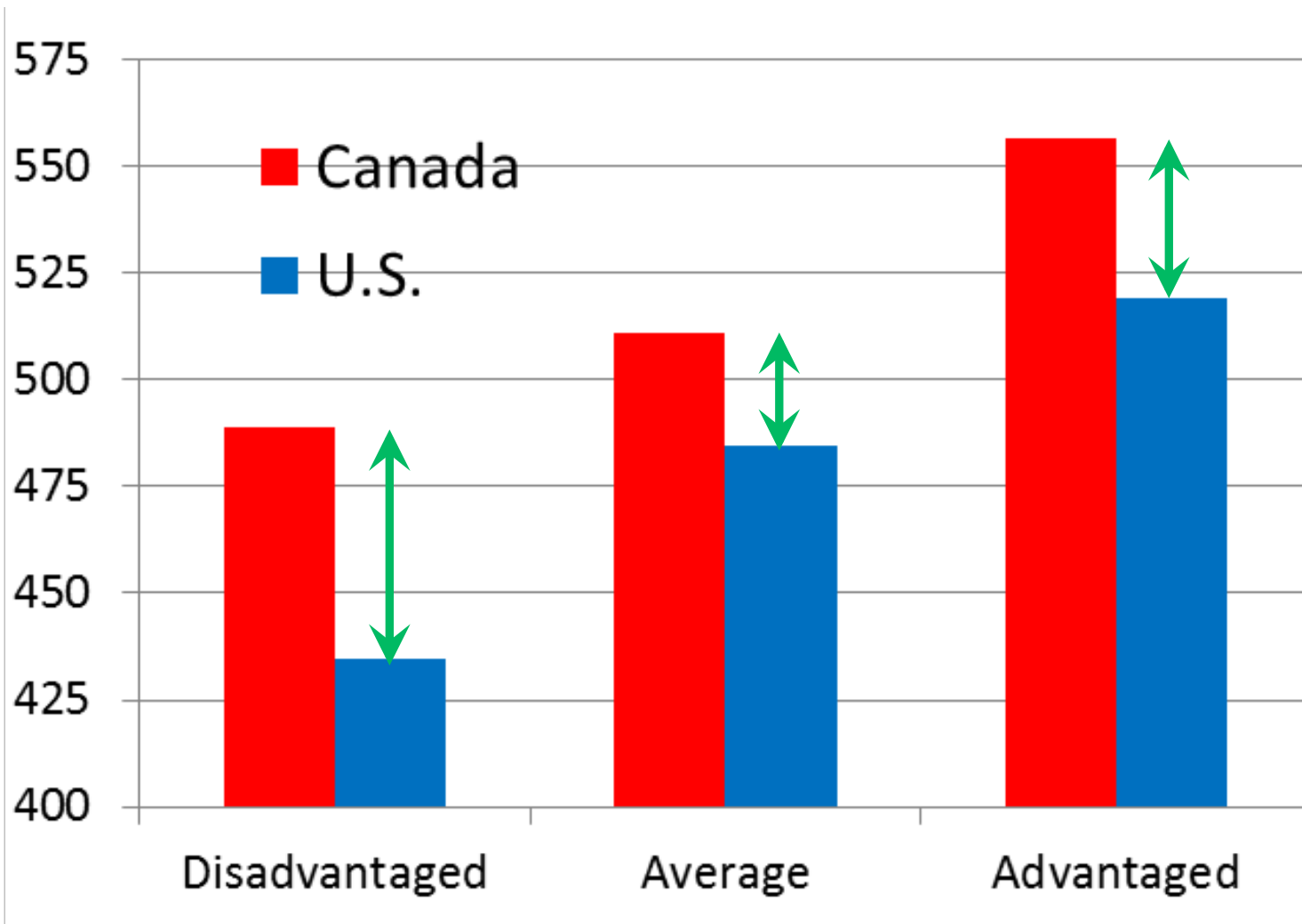
# Parental Influence – Father-Son Income Elasticities vs Gini

The Great Gatsby Curve: More Inequality is Associated with Less Mobility across the Generations



# “Neighbourhood” Influence – PISA Math Scores by Average School SES

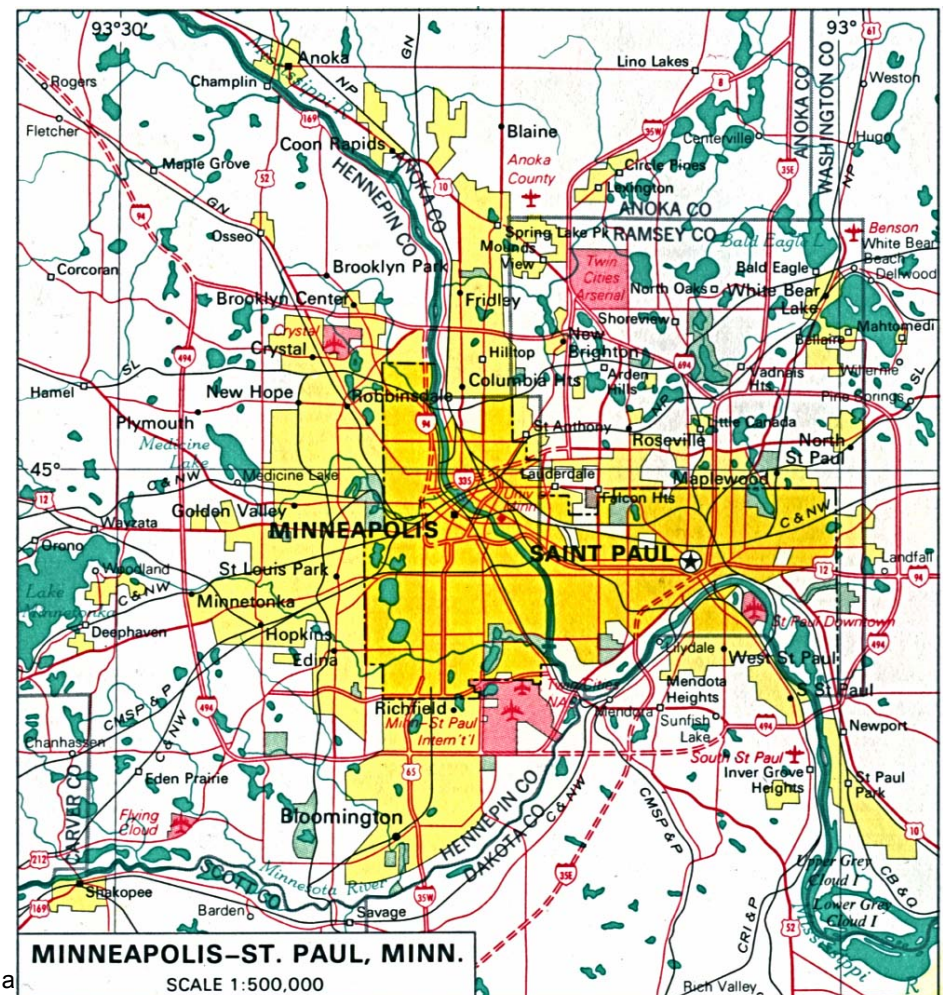
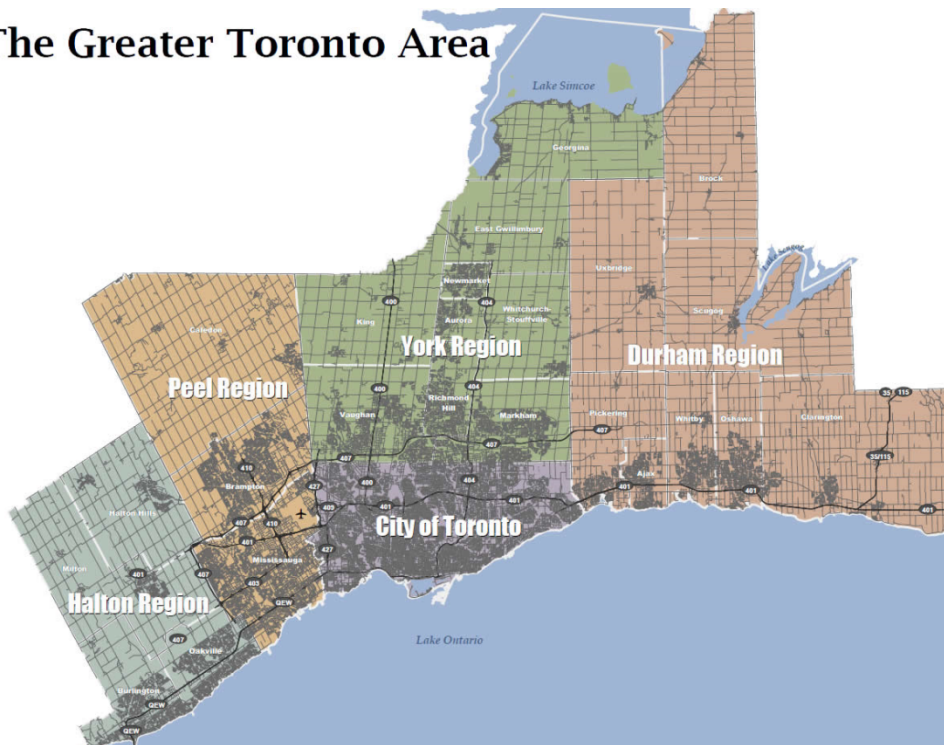
OECD, PISA 2012 Database, Table II.2.10



# City Structure: e.g. Minneapolis and Toronto

- 200+ versus ~15 elected governments (municipal, school boards, etc.)?
- differing extent of racial / economic segregation?
- comparable data lacking

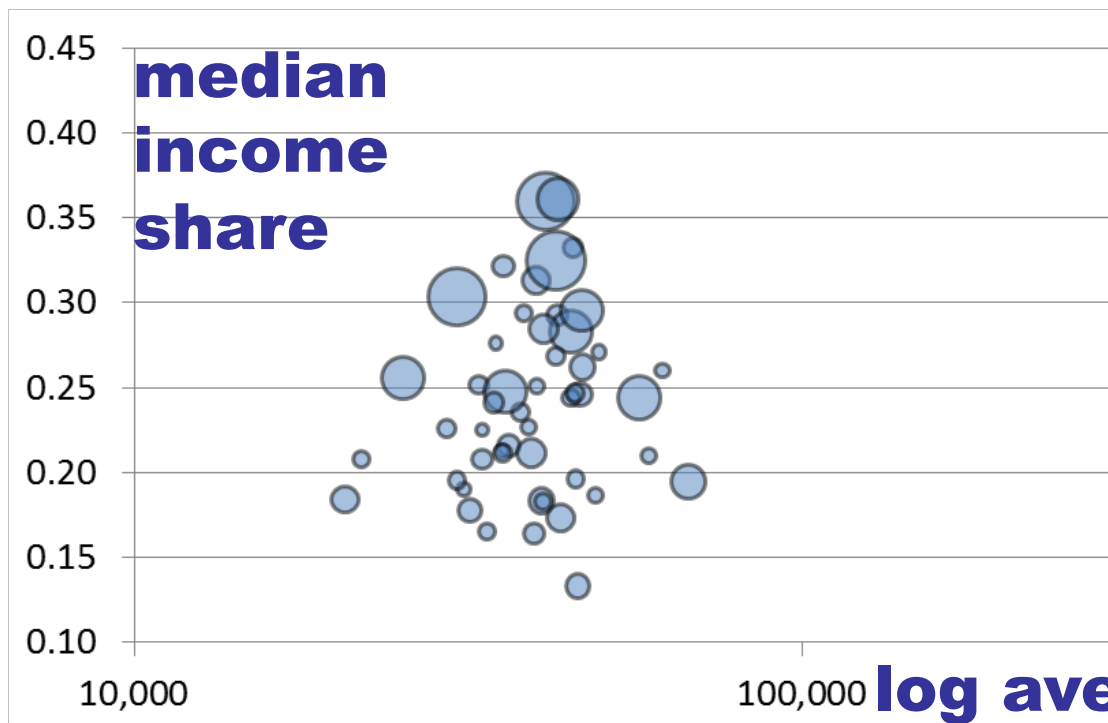
The Greater Toronto Area



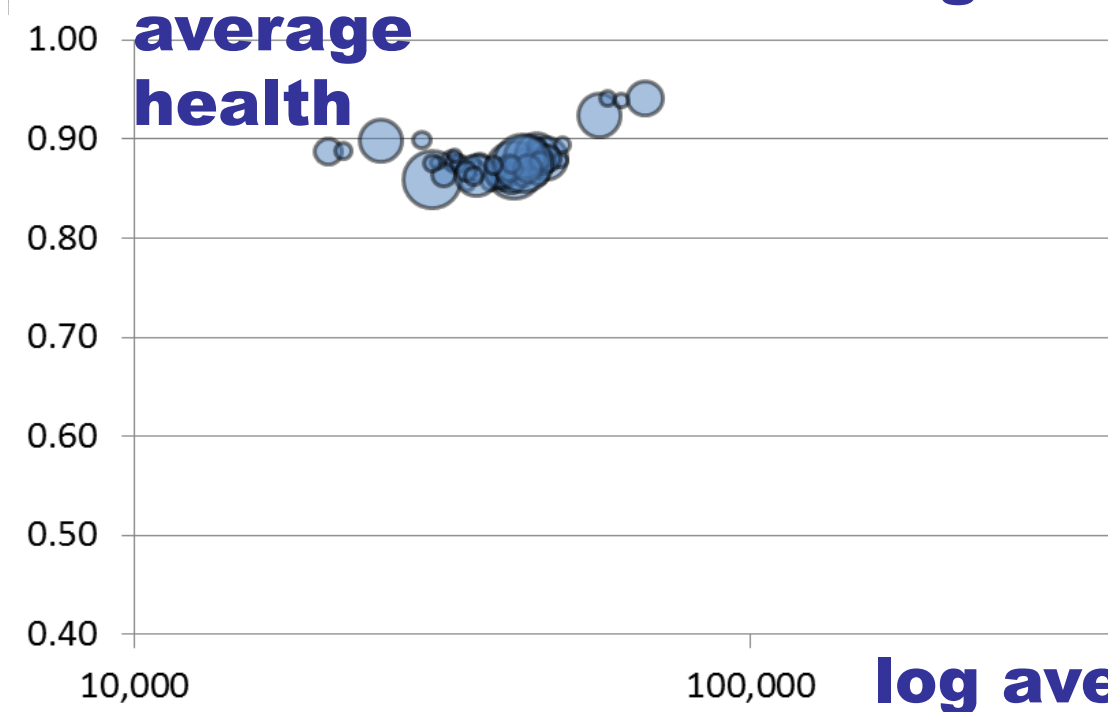
On validation...



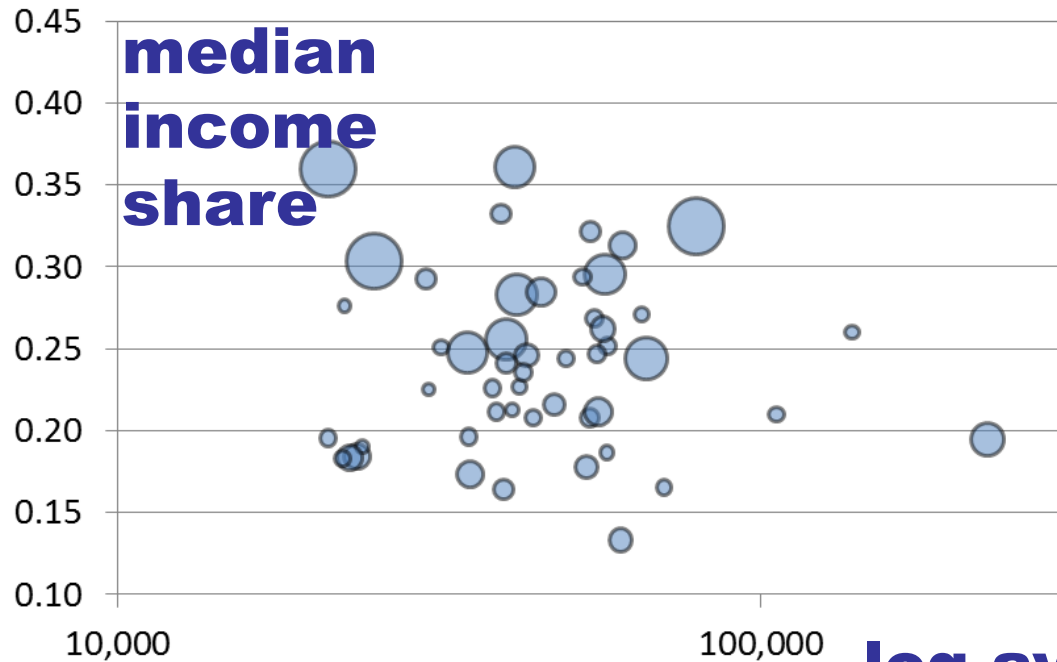




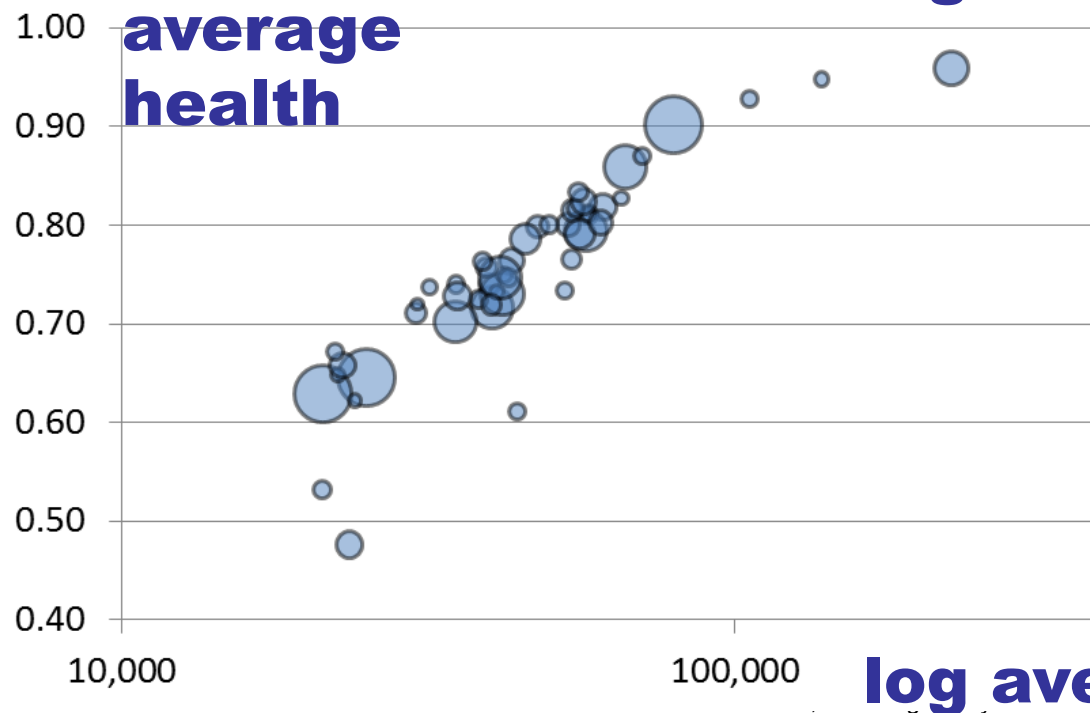
**100 Nbhds,  
Decade 1  
(areas proportional  
to population)**



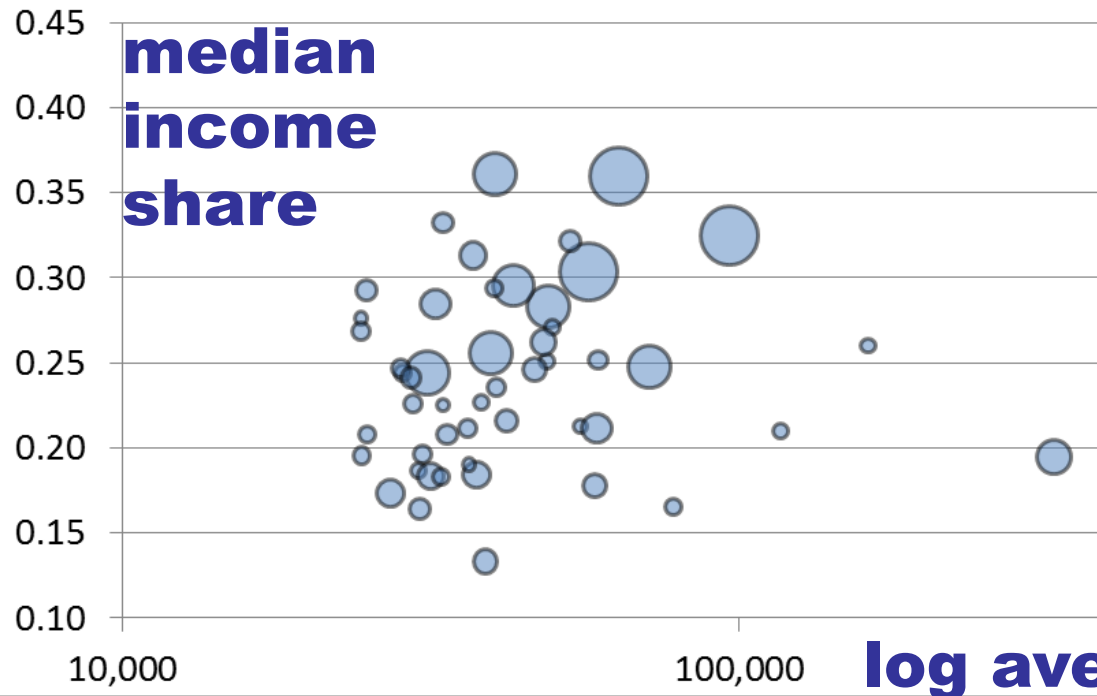
**population starts  
randomly  
distributed over  
nbhds and  
incomes, but all  
in very good  
health**



**100 Nbhds,  
Decade 5  
(areas proportional  
to population)**

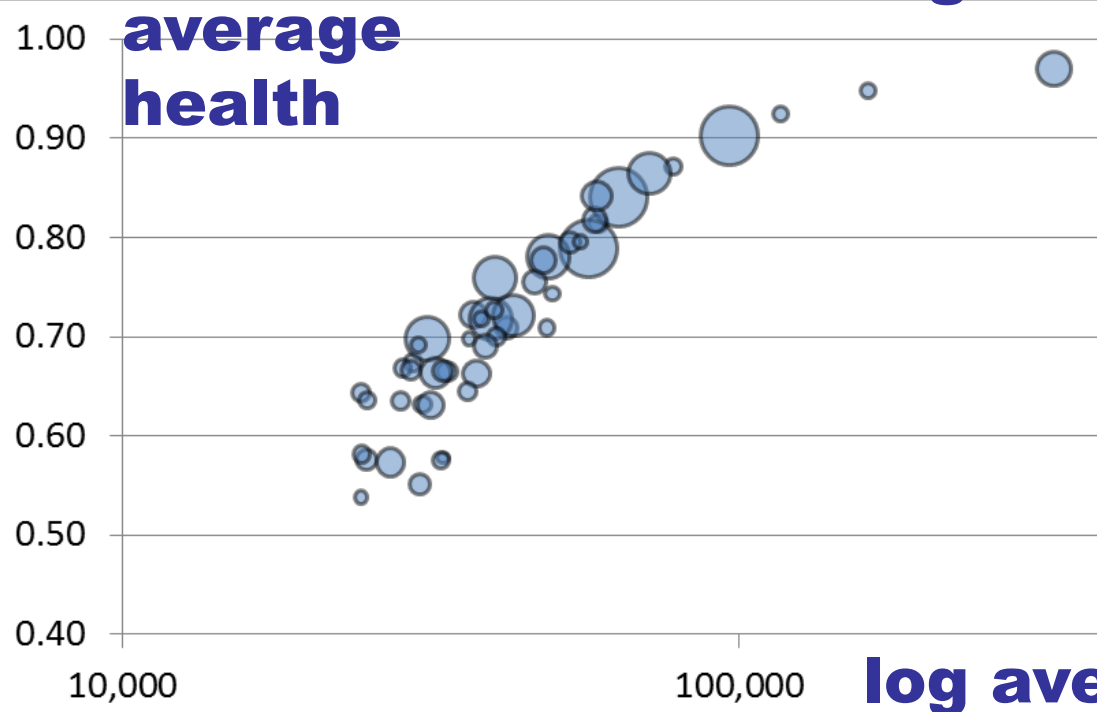


**by 5<sup>th</sup> decade, nbhds  
spread out in terms  
of average income,  
and health ↔  
income pattern  
emerges**



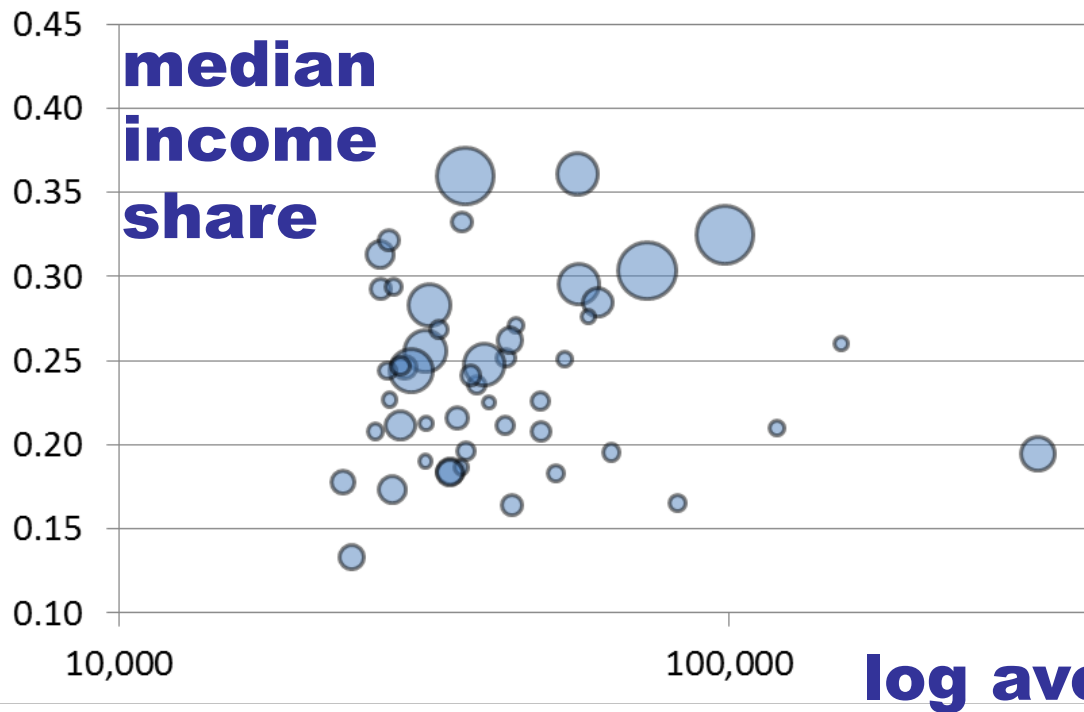
**100 Nbhds,  
Decade 10**  
(areas proportional  
to population)

**n.b. overall Gini  
not changing**



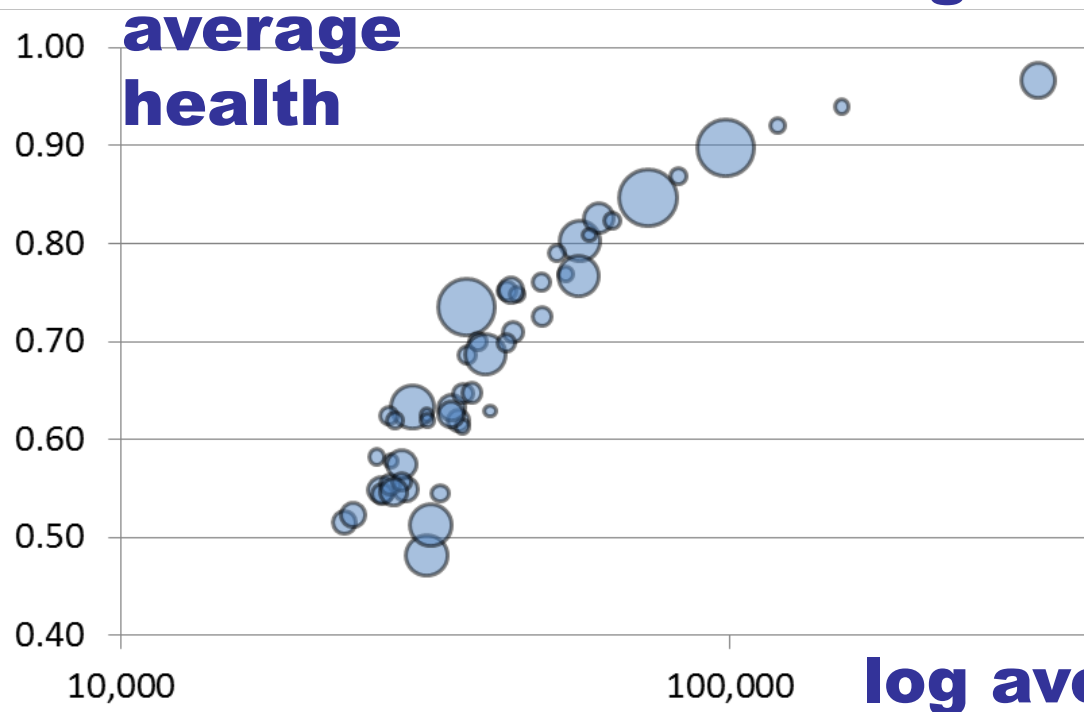
**n.b. nbhd  
health ↔  
income  
gradient  
becoming  
steeper**



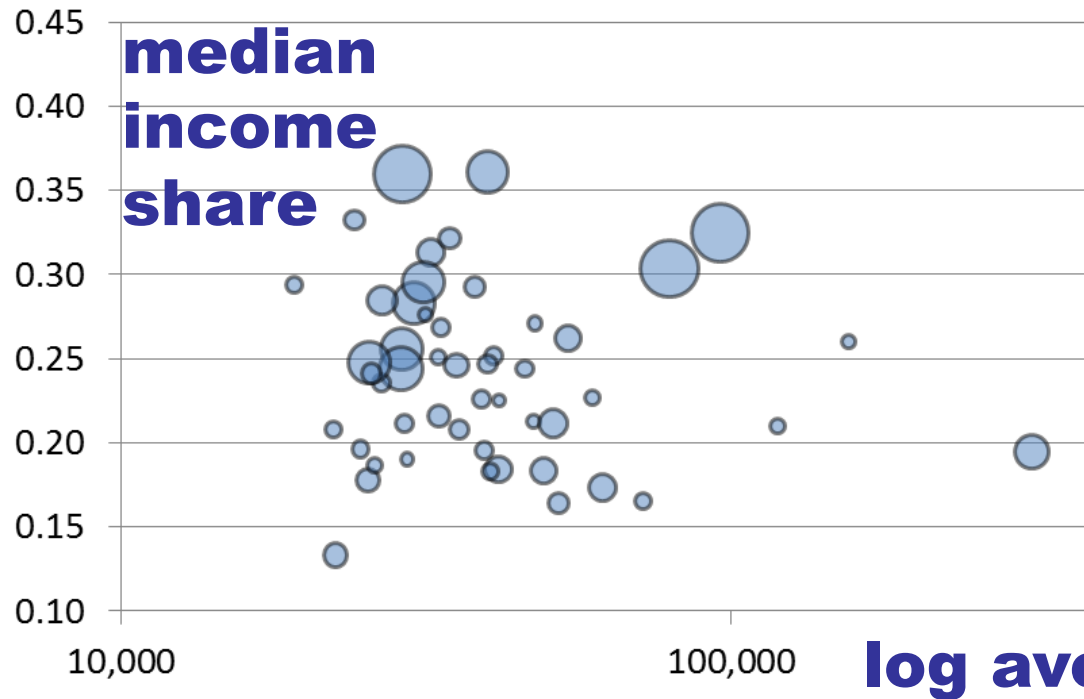


**100 Nbhds,  
Decade 20**  
(areas proportional  
to population)

**n.b. overall Gini  
not changing**

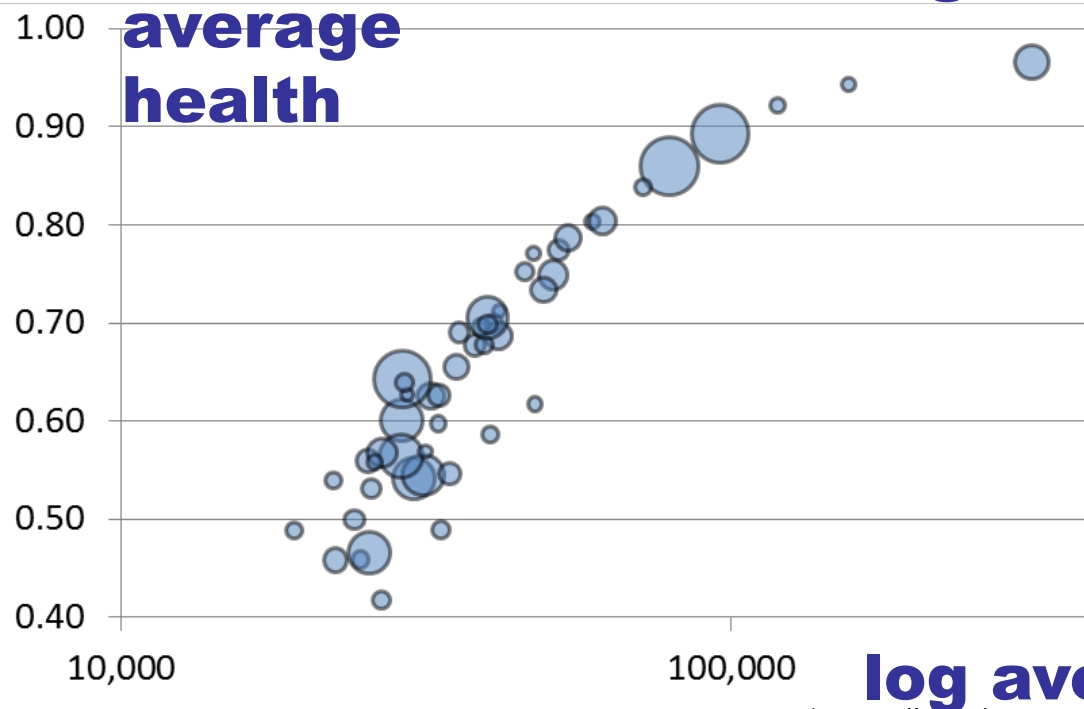


**n.b. nbhd  
health ↔  
income  
gradient  
becoming  
steeper**

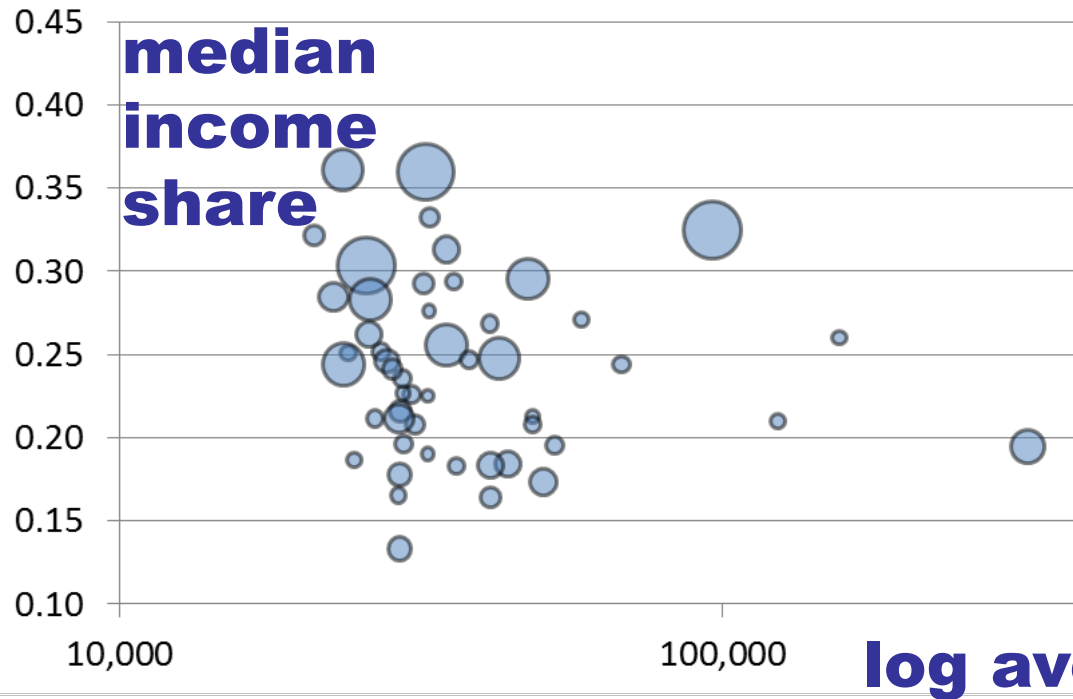


**100 Nbhds,  
Decade 30**  
(areas proportional  
to population)

**n.b. overall Gini  
not changing**

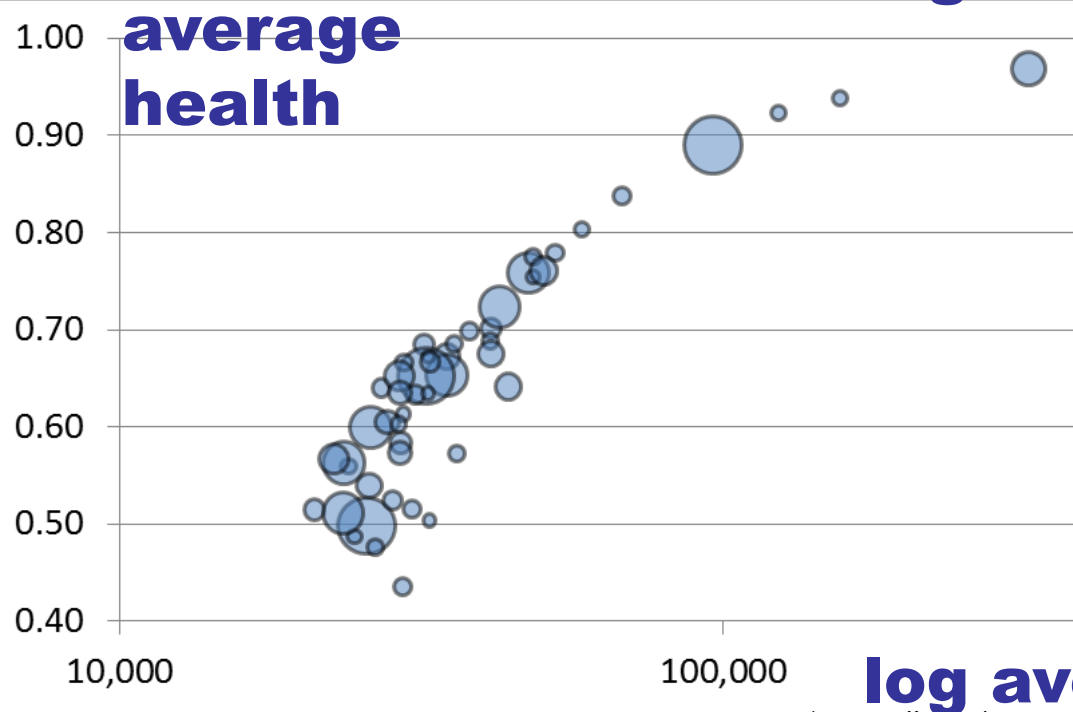


**n.b. nbhd  
health ↔  
income  
gradient  
becoming  
steeper**

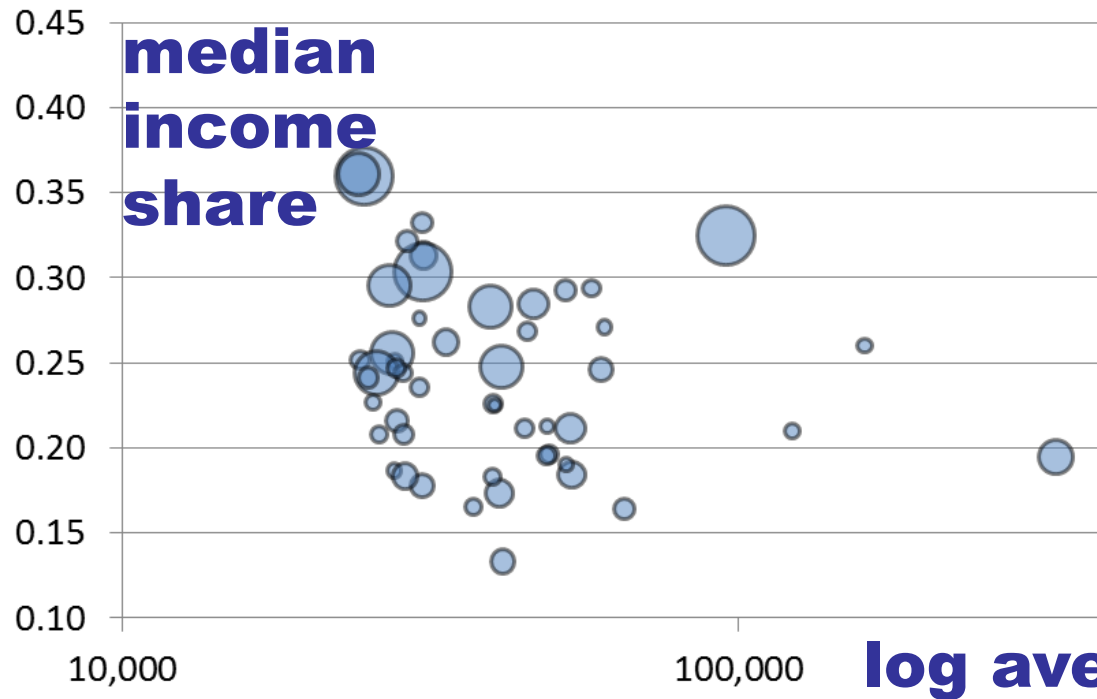


**100 Nbhds,  
Decade 40**  
(areas proportional  
to population)

**n.b. overall Gini  
not changing**

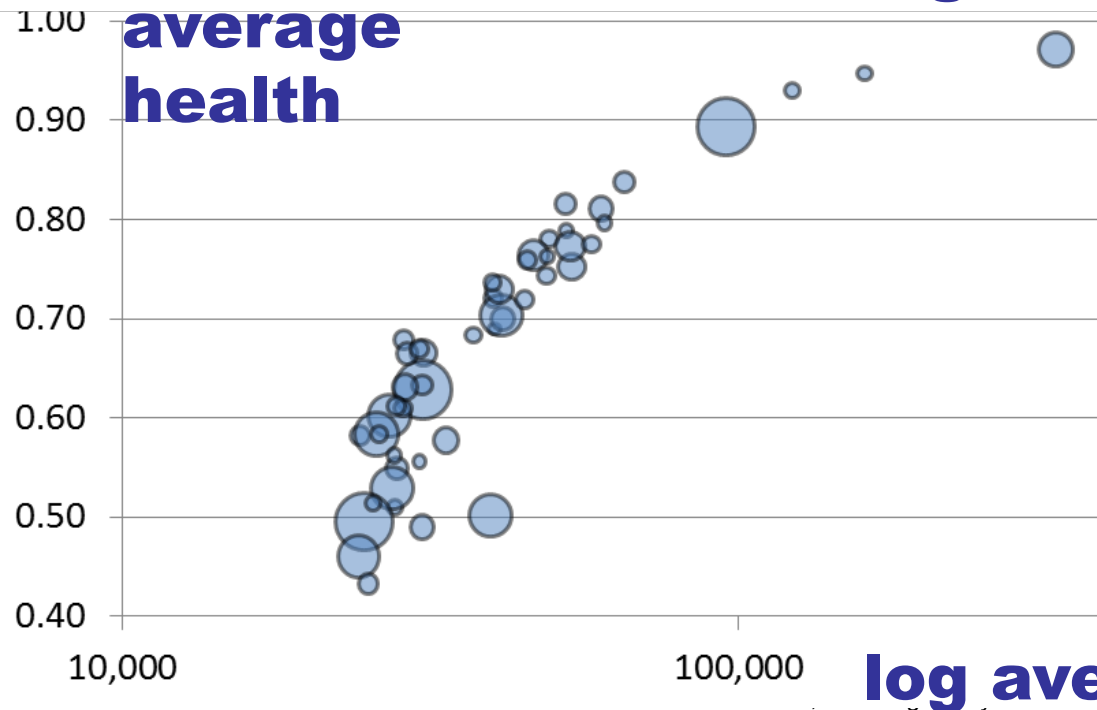


**n.b. nbhd  
health ↔  
income  
gradient  
becoming  
steeper**



**100 Nbhds,  
Decade 50**  
(areas proportional  
to population)

**n.b. overall Gini  
not changing**



**n.b. nbhd  
health ↔  
income  
gradient  
becoming  
steeper**

# On neighborhood dynamics over time...



# Simulated Health Gradients by Income and Selected 5 Year Age Groups

- average health declines with age
- gradient becomes steeper with age
- stochastic variation greatest in top age groups

